

# **Quantification of Turbulent Heat Fluxes and the Energy Balance Closure over a Flux Tower in the Semi-arid Savannah area of Naivasha, Kenya**

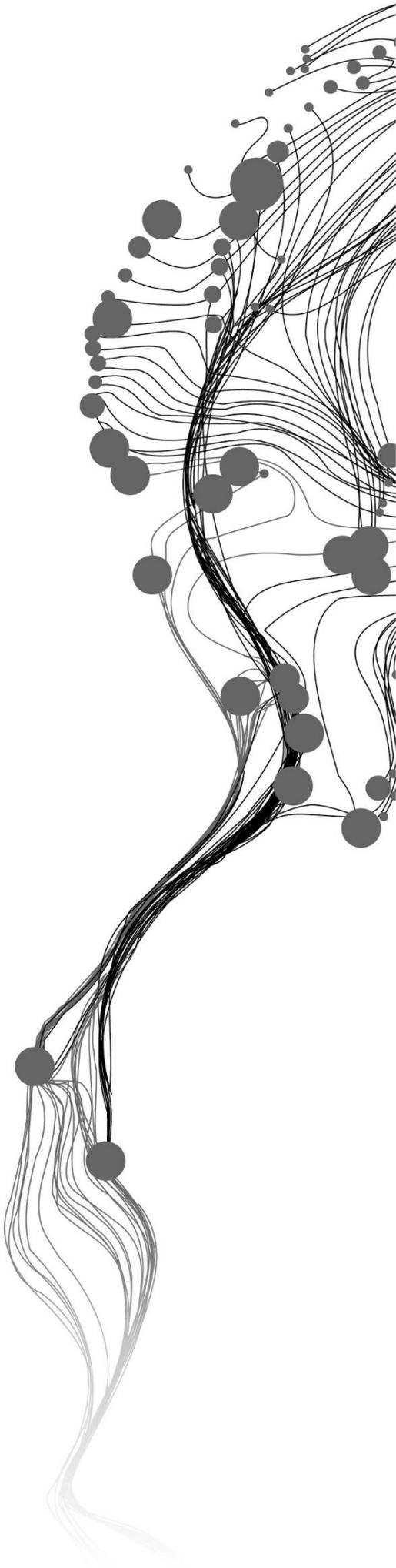
JOHN MBATHA MUTINDA

February, 2017

SUPERVISORS:

Dr. Ir. Christiaan Van der Tol

Drs. Robert Becht



# **Quantification of Turbulent Heat Fluxes and the Energy Balance Closure over a Flux Tower in the Semi-arid Savannah area of Naivasha, Kenya**

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Enschede, The Netherlands, February, 2017

Thesis submitted to the Faculty of Geo-Information Science and Earth Observation of the University of Twente in partial fulfilment of the requirements for the degree of Master of Science in Geo-information Science and Earth Observation.

Specialization: Water Resources and Environmental Management.

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#### DISCLAIMER

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# ABSTRACT

Quantification of turbulent heat fluxes is important as they influence regional and global climates. This becomes very vital in semi-arid ecosystems where evapotranspiration accounts for ~90% of rainfall losses. The dependability of quantified fluxes as inputs into climate and hydrological models is hinged on energy balance closure and therefore it is important to quantify and understand sources of lack of energy balance closure; which remains to be an unresolved problem with many eddy covariance systems.

In this study, half hourly turbulent heat fluxes are derived using measurements from a flux tower situated in a semi-arid savannah area of Naivasha, Kenya, between the year 2012 and 2014, and over a brief period in 2016. Given that this site is not a full eddy covariance system owing to lack of a gas analyzer, latent heat fluxes are derived by inversion of the Bowen ratio derived from relative humidity and temperature measurements. In combination with ground heat flux estimated from a soil heat flux plate and soil temperature profile measurements; the energy balance closure is computed. Causes of lack of energy balance closure are evaluated, specifically the effects of quality filtering based on friction velocity, effects of flux footprint, effects of Bowen ratio inter-calibration and accuracy in ground heat flux estimation. Representativeness of tower measured net radiation is also evaluated by comparing it with net radiation retrieved from Landsat 8 OLI & TIRS satellite.

The overall energy balance ratio (EBR) for three years analysed (2012-2014) was 58% , while yearly EBR's were 67% for 2012, 56% for 2013, 51% for 2014 and 49% for 2 months analysed in 2016. Quality filtering of fluxes when  $u^*$  is less than  $0.3 \text{ m s}^{-1}$  improved the overall EBR for the three years evaluated by 5%. Filtering fluxes emanating from a road surface towards the east of the tower when wind direction is between  $60^\circ$  -  $120^\circ$  improved the overall EBR further by 6%. Net radiation measured by the tower radiometer is found to be higher than net radiation retrieved from the satellite both at the tower pixel and when averaged over the tower source area. Correcting for the bias in net radiation improved the overall EBR by 5%. Combining filtering data when  $u^* < 0.3 \text{ m s}^{-1}$ , when wind direction is between  $60^\circ$  -  $120^\circ$  and correcting for bias in net radiation improved the overall EBR for three years (2012 – 2014) to 76% which is an 18% increase. Yearly EBRs increased to 83%, 77% and 69% for 2012, 2013 and 2014 respectively.

It is recommended that other possible factors attributed to lack of closure such as advection and averaging time that were not analysed in this study be evaluated. Further, it is recommended that a gas analyzer be added to the tower for more accurate measurements of latent heat fluxes.

**Keywords:** Energy Balance Closure, Flux Tower, Turbulent Heat Fluxes, Sensible Heat Flux, Latent Heat Flux, Ground Heat Flux, Energy Balance Ratio, Bowen Ratio, Inter-Calibration.

## DEDICATION

This work is dedicated to my dear mother Cecilia Kaluki, who sacrificed a lot and fought to ensure that I had the best education.

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# TABLE OF CONTENTS

---

|      |  |    |
|------|--|----|
| 1.   | INTRODUCTION.....  | 1  |
| 1.1. | Background.....  | 1  |
| 1.2. | Problem Statement.....                                     | 1  |
| 1.3. | Objectives .....   | 2  |
| 2.   | STUDY AREA .....   | 3  |
| 2.1. | Study Area.....  | 3  |
| 3.   | THEORETICAL BACKGROUND.....                                | 7  |
| 3.1. | The Energy Balance Closure Problem.....                    | 7  |
| 4.   | RESEARCH METHODOLOGY .....                                 | 9  |
| 4.1. | Methodology Flowchart .....                                | 9  |
| 4.2. | Data Quality Checks .....                                  | 9  |
| 4.3. | Turbulent Fluxes.....                                      | 10 |
| 4.4. | Inter-calibration of Bowen ratio measuring equipment ..... | 11 |
| 4.5. | Ground Heat Flux.....                                      | 12 |
| 4.6. | Energy Balance Closure .....                               | 13 |
| 5.   | RESULTS AND DISCUSSION .....                               | 19 |
| 5.1. | Diurnal Variation of Fluxes.....                           | 19 |
| 5.2. | Energy Balance Closure .....                               | 20 |
| 6.   | CONCLUSION AND RECOMMENDATIONS.....                        | 33 |
| 6.1. | Conclusion.....  | 33 |
| 6.2. | Recommendations.....                                       | 33 |
|      | APPENDICES .....   | 39 |

## LIST OF FIGURES

---

|  |    |
|--|----|
| Figure 2.1: Location of flux tower. The tower is marked with a star. T and R refer to the transmitter and receiver of the scintillometer respectively (Odongo et al., 2016). .....   | 3  |
| Figure 2.2: Photograph of Naivasha flux tower taken on 23/9/2016 showing different instrumentations and views in different directions.....   | 5  |
| Figure 4.1: Methodology Flowchart.....   | 9  |
| Figure 4.2: Regression plots used to obtain equations used for RH and T inter-calibration correction. The blue line indicates 1:1 relationship.....  | 11 |
| Figure 5.1: Hourly averaged fluxes showing diurnal flux variations in the year 2012. The closure term is shown in purple. ....   | 19 |
| Figure 5.2: Linear regressions of $R_n-G_0$ vs $H+LE$ for 2012 – 2014 and April 4 <sup>th</sup> – June 3 <sup>rd</sup> 2016. Regression lines have been forced through the origin .....  | 21 |
| Figure 5.3: 2016 (April 4 <sup>th</sup> -June 3 <sup>rd</sup> ) after Bowen ratio intercalibration .....   | 22 |
| Figure 5.4: Rose diagram showing wind direction for period between 2012 and 2014. The colour bar indicates wind speeds ( $m\ s^{-1}$ ) .....   | 23 |
| Figure 5.5: Midday flux footprint for 17/07/2013 overlaid on a true colour Google Earth image. The red intensity colour shows the highest contribution area, followed by the yellow, the cyan and the purple. The tower location is shown with a star. ....  | 24 |
| Figure 5.6: Three year climatology footprint (2012-2014). The middle high intensity colour represents highest contribution area. The contribution area reduces with decreasing colour intensity.....   | 24 |
| Figure 5.7: Polar plot of EBR vs Wind direction for the period between 2012 and 2014. ....   | 25 |
| Figure 5.8: Comparison of G derived using measurements from soil heat flux plates installed in different directions (Note: South plate is at 10cm while all others are at 5cm).....  | 26 |
| Figure 5.9: Net radiation maps derived from Landsat 8 OLI & TIRS for 22/11/2013 and 17/05/2014. The maps show spatial variability in net radiation over the study area. ....   | 27 |
| Figure 5.10: Comparisons of tower measured and satellite derived net radiation ( $R_n$ ). (a) shows comparison with tower pixel value while (b) shows comparison with net radiation aggregated over the tower footprint area. The dashed line shows the 1:1 relationship.....  | 28 |
| Figure 5.11: Linear regression of $R_n-G_0$ against $H+LE$ for the year 2012, 2013, 2014 and 2016 together with the three year overall 2012-2014; after combined filtering of data when $u^* < 0.3\ ms^{-1}$ , when wind direction is between $60^\circ - 120^\circ$ and correcting for the bias in net radiation. The regression lines have been forced through the origin..... | 30 |
| Figure 5.12 Comparison between Latent heat from Bowen ratio and latent heat measured by a gas analyzer for the days the gas analyzer was working.....  | 31 |
| Figure 5.13: Linear regressions of $H+LE$ vs $R_n-G_0$ using LE measured by gas analyzer and using LE derived from Bowen ratio.....  | 31 |
| Figure 5.14: Linear regressions of $H+LE$ vs $R_n-G_0$ using LE measured by gas analyzer and using LE derived from Bowen ratio after combined data filtering discussed in Section 5.2.6 .....  | 32 |

## LIST OF TABLES

---

|   |    |
|---|----|
| Table 2.1: Flux tower instrumentation (Odongo et al., 2016).....  | 4  |
| Table 2.2: Summary of data sets.....  | 5  |
| Table 2.3: Description of Landsat 8 OLI and TIRS bands (USGS, 2016).....  | 6  |
| Table 4.1: Coefficients from TIGR61 database for estimating atmospheric transfer functions (AF's) .....   | 15 |
| Table 4.2: Total column water vapour estimates retrieved from ECMWF: .....  | 16 |
| Table 5.1: Monthly averaged energy partitions for the period between 2012 and 2014. Closure term(C) is also shown .....   | 20 |
| Table 5.2: Summary of regression coefficients of Rn-G0 vs H+LE, EBRs and RMSEs for 2012 – 2014 and April 4 <sup>th</sup> – June 3 <sup>rd</sup> 2016.....   | 21 |
| Table 5.3: Summary of Slopes of linear regression of Rn-G0 vs H+LE, EBRs and RMSEs after filtering fluxes when $u^* < 0.3 \text{ m s}^{-1}$ .....   | 23 |
| Table 5.4: Summary of Slopes of linear regression, EBRs and RMSEs after filtering fluxes when wind direction was between $60^\circ$ and $150^\circ$ .....   | 25 |
| Table 5.5: Standard deviation of Ground heat flux measurements from the four additional plates in comparison with the plate to the south. ....  | 26 |
| Table 5.6: Summary of Coefficients of linear regression of H+LE vs Rn-G0, EBRs and RMSEs after correcting for bias in Rn.....   | 29 |
| Table 5.7: Summary of linear regressions coefficients, EBRs and RMSEs after combined filtering of data when $u^* < 0.3 \text{ m s}^{-1}$ , filtering when wind direction between $60^\circ$ - $120^\circ$ and correcting for bias in net radiation..... | 29 |

## LIST OF ABBREVIATIONS

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|        |  |
|--------|--|
| AFs    | Atmospheric transfer Functions                     |
| AMMA   | African Monsoon Multi-disciplinary Analysis        |
| DN     | Digital Number                                     |
| DOS    | Dark Object Subtraction                            |
| EBR    | Energy Balance Ratio                               |
| ECMWF  | European Centre for Medium-Range Weather Forecasts |
| ENVI   | ENvironment For Visualizing Images                 |
| ET     | Evapotranspiration                                 |
| ETM    | Enhanced Thematic Mapper                           |
| FFP    | Flux Footprint Prediction                          |
| FVC    | Fractional Vegetation Cover                        |
| HAPEX  | Hydrology Atmosphere Pilot Experiment              |
| ILWIS  | Integrated Land and Water Information System       |
| KWSTI  | Kenya Wildlife Service Training Institute          |
| LE     | Latent Heat  |
| LSE    | Land Surface Emissivity                            |
| LST    | Land Surface Temperature                           |
| MATLAB | Matrix Laboratory                                  |
| MODIS  | Moderate Resolution Imaging Spectroradiometer      |
| NDVI   | Normalized Difference Vegetation Index             |
| NIR    | Near Infrared                                      |
| OLI    | Operational Land Imager                            |
| QGIS   | Quantum Geographic Information System              |
| RH     | Relative Humidity                                  |
| RHT    | Relative Humidity and Temperature                  |
| RMSE   | Root Mean Square Error                             |
| TIGR61 | TOVS Initial Guess Retrieval                       |
| TIRS   | Thermal Infrared Sensor                            |
| TOA    | Top of the Atmosphere                              |
| USGS   | United States Geological Survey                    |
| VIS    | Visible  |
| WRMA   | Water Resources Management Authority               |

# 1. INTRODUCTION

## 1.1. Background

Turbulent fluxes transport gases, energy and other substances in the atmospheric boundary layer at different scales both spatially and temporally (Zhang et al., 2014). In order to understand surface atmosphere interactions, it is important to quantify and partition turbulent fluxes since they influence local, regional and global climates making them crucial in eco-hydrological, weather and climate studies (Dirmeyer, 1994). In arid and semi-arid regions particularly, 90% of annual precipitation is lost as evapotranspiration (ET) (Huxman et al., 2005), making latent heat (LE) a major component of the energy balance. Quantification of turbulent fluxes and the energy balance for such ecosystems is thus important (Odongo et al., 2016).

Several methods have been developed for flux quantifications, amongst them the Bowen ratio method, the aerodynamic gradient method and the eddy covariance method. The Bowen ratio and Aerodynamic gradient are indirect methods and involve measurements at two heights. Though they use simple equipment, they may not be able to measure very small gradients in temperature. The eddy covariance method on the other hand is a direct method that involves measurement at one height (Moncrieff et al. (1997).

Eddy covariance measurement systems are currently the most preferred for quantification of turbulent fluxes, following their development over the last two decades, especially because such systems can also be used to quantify CO<sub>2</sub> fluxes (Evans et al., 2012). These systems have however been associated with the problem of energy imbalance as discussed by Foken et al. (2006); and to increase the dependability of fluxes measured by eddy covariance systems, it is important to determine and understand the source of these imbalances (Twine et al., 2000).

This study is therefore aimed at quantifying turbulent fluxes and analyzing the energy balance using flux measurements taken by an eddy covariance system installed in a semi-arid savannah area of Naivasha, Kenya, with a specific focus of investigating the sources of lack of energy balance closure. This site relies on Bowen ratio method for estimation of Latent heat fluxes as a gas analyzer is not permanently installed, apart from a 40 day period during the year 2012.

## 1.2. Problem Statement

The number of measurements of energy fluxes in heterogeneous savannah ecosystems is limited (Kurc & Small, 2004). In the case of East Africa particularly, these limitations are aggravated by lack of adequate instrumentation for long term measurements and studies. For the first time in this region, long term flux measurements are now available through a flux tower installed at the Naivasha savannah in Kenya, which has been recording micro-meteorological and flux measurements since the year 2012. Odongo et al. (2016) presents the first analysis of energy fluxes using measurements from this tower. With 3 year data recorded between the years 2012 and 2014, they report an energy balance ratio of 0.65. A detailed analysis to determine the source of low closure has however not been carried out. Lack of energy balance closure in eddy covariance measurement systems has been reported in many studies. Errors of 10-30% are common (Sánchez, Caselles, & Rubio, 2010). Such energy imbalance has an impact on the interpretation and

application of the measured fluxes and how they compare to modelled estimates. It is therefore important to determine, understand and explain the source of this low closure (Twine et al., 2000).

### **1.3. Objectives**

#### **1.3.1. Main Objectives**

To quantify turbulent heat fluxes and analyze the causes of the energy balance closure error using measurements taken by a flux tower in the semi-arid savannah area of Naivasha, Kenya; between 2012 and 2014.

#### **1.3.2. Specific Objectives**

1. To determine the energy balance closure.
2. To determine the effects of quality filtering of data for underdeveloped turbulence based on friction velocity.
3. To investigate whether the flux footprint extends into the nearby urban area, and the effect of this on energy balance closure.
4. To investigate the effect of errors in Bowen ratio measurements on the energy balance closure.
5. To investigate the measurement accuracy of ground heat flux, the representativeness of net radiation and its effect on the energy balance closure.

#### **1.3.3. Research Questions**

1. What is the energy balance closure of flux measurements taken between 2012 and 2014?
2. What is the effect of filtering data for underdeveloped turbulence based on friction velocity on the energy balance closure?
3. What is the effect of Bowen ratio measurement errors due to accuracy and precision of the temperature and relative humidity instruments on the energy balance closure?
4. Is there an error in the estimation of ground heat flux and how does this affect the energy balance closure?
5. How representative is net radiation measured by the tower radiometer in reference to the turbulent fluxes source area?

## 2. STUDY AREA

### 2.1. Study Area

The flux tower is located within the L. Naivasha basin in Kenya as shown in Figure 2.1. It is inside a protected area which hosts the Kenya Wildlife Service Training Institute (KWSTI).

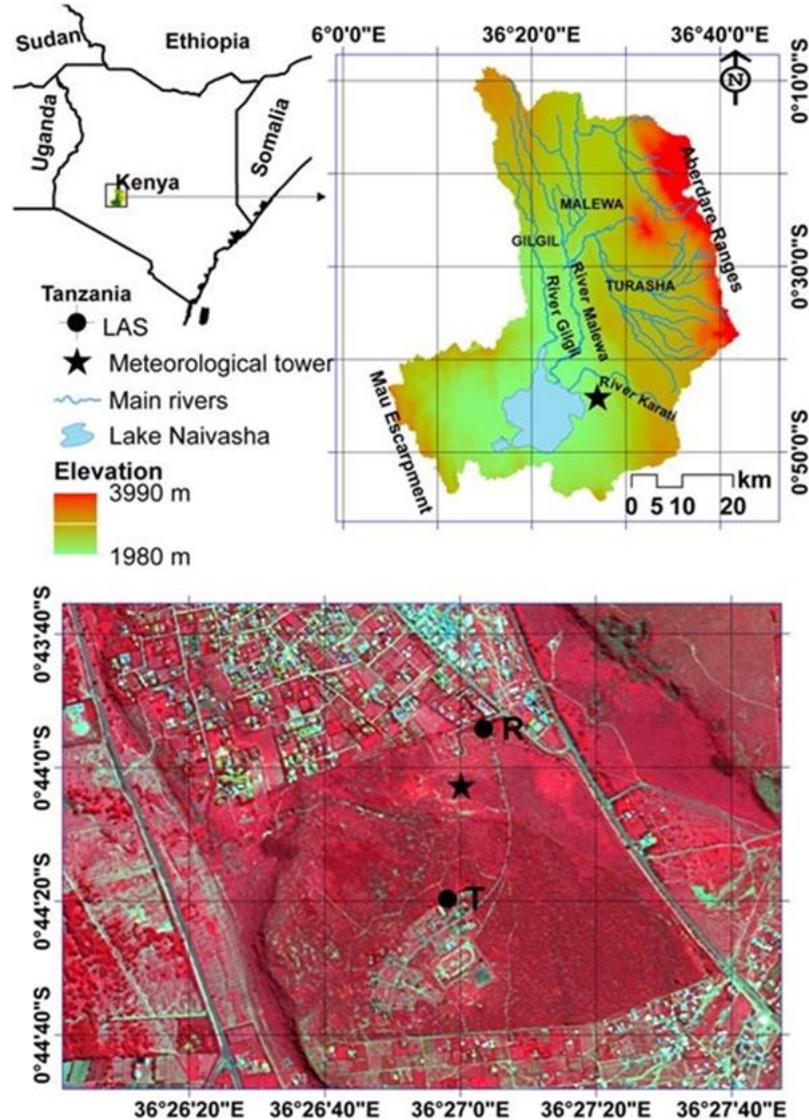


Figure 2.1: Location of flux tower. The tower is marked with a star. T and R refer to the transmitter and receiver of the scintillometer respectively (Odongo et al., 2016).

#### 2.1.1. Climate and Vegetation

The study area is at an elevation of  $\sim 2000\text{m}$  above sea level. Lake Naivasha catchment in which the tower is located experiences two rainy seasons. Long rains occur between March and May, while short rains occur between October and December. The area receives an average rainfall of  $610\text{mm}$  per annum. Vegetation of the area is characterized by shrubs and a few scattered trees with a grass cover of 40-60%. Shrubs exhibit a general height of 0.5-1m. Shrubs shed leaves and grass dries during the dry season, then

sprouting occurs shortly after the rains. The flux tower site is generally flat with a gentle slope towards the lake on the West. The terrain goes up towards the East. (Odongo et al., 2016).

### 2.1.2. Instrumentation

The flux tower has a height of 5.5 metres and is installed with the instruments described in Table 2.1. It has been operational since January 2012.

Table 2.1: Flux tower instrumentation (Odongo et al., 2016).

| No. | Instrument description   | Parameter   |
|-----|--|---|
| 1.  | 3D sonic anemometer (WindMaster (Pro) type 1516, Gill Instruments Limited, Hampshire, UK).<br>-Sampling frequency 10Hz                                   | Wind velocity,<br>Virtual temperature fluctuations  |
| 2.  | HFM53, Rotronic Instruments (UK) Limited, West Sussex, UK)   | Aspirated air temperature & relative humidity at 1.8m and 5.5m above ground level<br>-Enables Bowen ratio computation |
| 3.  | NR101 four component radiometer (Hukseflux, Delft, The Netherlands)<br>-At 2.5m above the ground   | Downward and upward solar and long wave radiation   |
| 4.  | 10k $\Omega$ NTC (Campbel-107, Campbell Scientific Inc., Logan, UT, USA)<br>-Installed at 1, 2, 3, 4, 5, 6, 7, 8, 10 and 12.5 cm depths below the ground | Soil temperature profiles   |
| 5.  | Decagon EM50 5ET soil moisture sensors(Decagon Devices Inc., Washington, USA)  | Soil water content  |
| 6.  | Dielectric leaf wetness sensor (LWS-L Campbell Scientific Inc., Logan, UT, USA)  | Dew presence  |
| 7.  | Infra-red remote temperature sensor (IR100 Campbell Scientific Inc., Logan, UT, USA)   | Surface temperature   |
| 8.  | Soil Heat Flux Plate (HFP01SC, Hukseflux, Delft, The Netherlands)<br>-Installed at 10cm depth below the ground   | Soil heat fluxes  |
| 9.  | Tipping bucket rain gauge ( Rain Collector II, Davis Instruments, USA)   | Rainfall  |

All the instruments are connected to a CR3000 data logger (Campbell Scientific Inc., Logan, UT, USA); apart from soil moisture sensors which are connected to a separate data logger. Soil heat fluxes are recorded at intervals of 15 minutes, soil water content at 30 minutes and other hydro-meteorological variables at 1 minute. A gas analyzer (LI-7500, Li-COR Biosciences, Nebraska, USA) was introduced between 21/03/2012 and 9/05/2012. It was installed at 5.5m above the ground and recorded at 10Hz. A large aperture scintillometer (Scintec BLS 450) with a propagation length of 810m was also installed at 6.85 metre path height above the ground. It operated between 7/02/2012 and 4/12/2012, but it did not take continuous measurements due to intermittent failures. Figure 2.2 shows some of the flux tower instrumentation and views of the immediate vicinity in different directions.

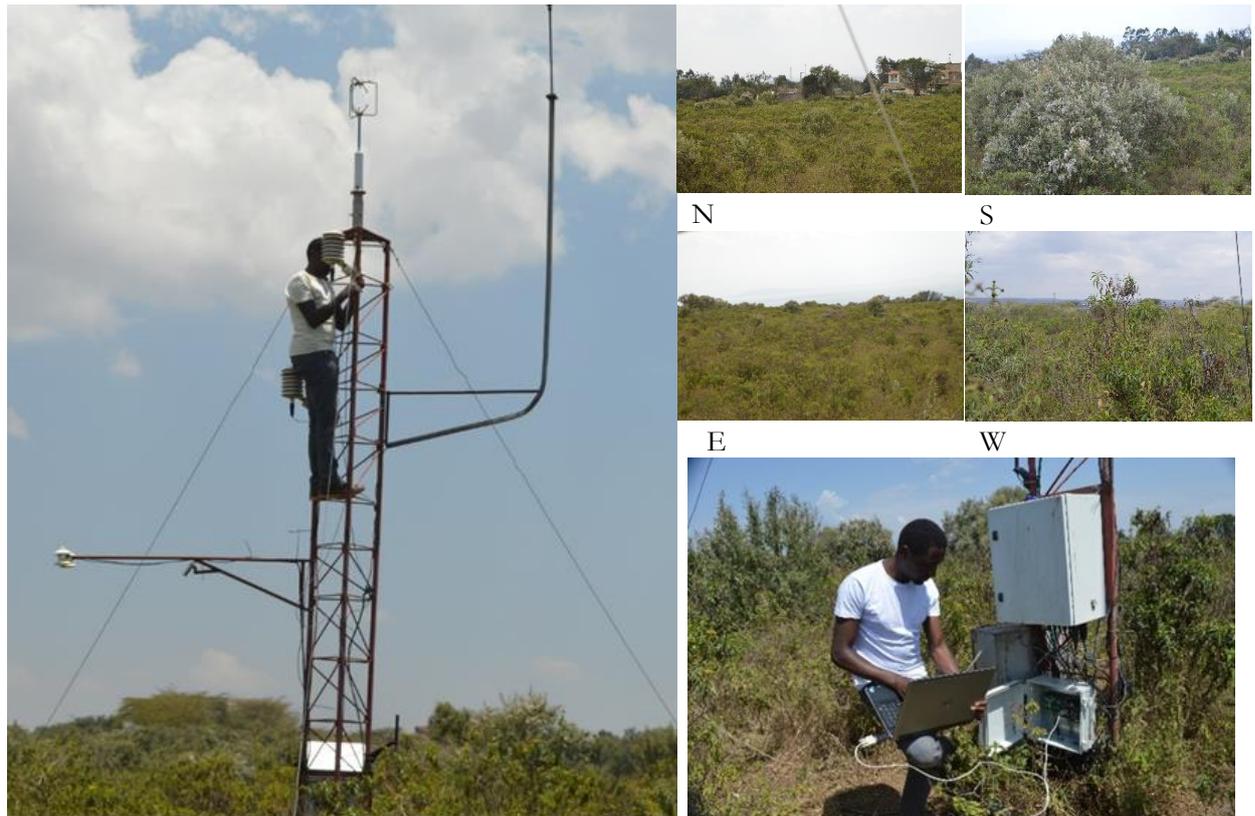


Figure 2.2: Photograph of Naivasha flux tower taken on 23/9/2016 showing different instrumentations and views in different directions.

### 2.1.3. Field Work and Data Collection

Field work was conducted between September 13th and October 4th 2016. Site visits, data acquisition and inspection of the general condition of the tower instrumentation was done during this period. Data for inter-calibration of the Bowen ratio measuring instruments was acquired by mounting the two set of Relative Humidity and Temperature (RHT) sensors at the same height and taking measurements for 5 days. In addition to the already existing soil heat flux plate, four soil heat flux plates (HFP01SC, Hukseflux, Delft, The Netherlands) were installed radially around the tower in the NW, SW, NE and SE directions, each at a depths of 5cm. The flux plates were connected to a separate CR1000 data logger and recorded measurements at 10 minute intervals. Long term flux measurements from the year 2012 to 2014 were obtained from Vincent Odongo. A summary of the data used for this study is shown in Table 2.2.

Table 2.2: Summary of data sets

| No. | Data Set                                   | Source   |
|-----|--|--|
| 1.  | Flux tower measurements                    | Data loggers on site, Vincent Odongo.  |
| 2.  | Landsat 8 OLI & TIRS images                | Downloaded from <a href="http://earthexplorer.usgs.gov/">http://earthexplorer.usgs.gov/</a>                |
| 3.  | Bowen ratio inter-calibration measurements | Field work: Mounting the humidity and temperature sensors at same level and taking measurements for 2 days |
| 4.  | Ground heat flux validation measurements   | Field work   |

#### 2.1.4. Satellite Data

Landsat 8 Operational Land Imager (OLI) and Thermal Infrared Sensor (TIRS) images were downloaded from <http://earthexplorer.usgs.gov/> using QGIS, an open source software. A total of 11 images (path 169 and row 60), with cloud cover less than 10% for the period between July 2013 and December 2014 were downloaded. Landsat 8 OLI and TIRS images consist of 9 bands with a spatial resolution of 30 metres for band 1 to 7 and band 9. Thermal bands 10 and 11 are collected at 100metres but resampled to 30 metres (USGS, 2016). The panchromatic band (band 8) is at 15metres resolution. Landsat 8 was launched in February 11th 2013 and it reached operational orbit on April 11th 2013. Table 2.3 shows a summary of description of Landsat 8 bands and their wavelength ranges.

Table 2.3: Description of Landsat 8 OLI and TIRS bands (USGS, 2016).

| <b>Band</b> |                             | <b>Wavelength [<math>\mu\text{m}</math>]</b> |
|-------------|-----------------------------|--|
| Band 1      | - Coastal aerosol           | 0.43 – 0.45                                  |
| Band 2      | - Blue                      | 0.45 – 0.51                                  |
| Band 3      | - Green                     | 0.53 – 0.59                                  |
| Band 4      | - Red                       | 0.64 – 0.67                                  |
| Band 5      | - Near Infrared(NIR)        | 0.85 – 0.88                                  |
| Band 6      | - SWIR 1                    | 1.57 – 1.65                                  |
| Band 7      | - SWIR 2                    | 2.11 – 2.29                                  |
| Band 8      | - Panchromatic              | 0.50 – 0.68                                  |
| Band 9      | - Cirrus                    | 1.36 – 1.38                                  |
| Band 10     | - Thermal Infrared (TIRS) 1 | 10.60 – 11.19                                |
| Band 11     | - Thermal Infrared (TIRS) 2 | 11.50 – 12.51                                |

### 3. THEORETICAL BACKGROUND

Turbulent heat fluxes between the land and the atmosphere influence weather and climate processes at global, regional and local scales, and it is therefore important to understand the processes by which the flux exchanges occur. In arid and semi-arid ecosystems, about 90% of annual precipitation is lost as ET making quantification and partitioning of turbulent heat fluxes vital for the hydrology of such areas (Odongo et al., 2016).

In the past, methods such as the aerodynamic gradient and the Bowen ratio have been used to study fluxes. With the development of sonic anemometers, the eddy covariance method has become a preferred method of quantifying turbulent fluxes (Moncrieff et al., 1997).

The first coordinated eddy covariance systems were by EUROFLUX as detailed by Aubinet et al. (1999) followed by AMERIFLUX. Success of the two led to implementation of the FLUXNET, a global system of eddy covariance towers mostly over Europe, North and South America, parts of Asia, and a few locations in Africa (Baldocchi et al., 2001).

In Africa, several studies have been conducted, amongst them the African Monsoon Multidisciplinary Analysis (AMMA) extensively described by Redelsperger et al., (2006) and the HAPEX-Sahel (Goutorbe et al., 1997). Measurements over East Africa are however very limited due to lack of proper instrumentation for long term measurements. Odongo et al. (2016) presented the first known ‘long term’ (i.e., multiple-years) flux measurements in this region through a flux tower installed in the semi-arid savannah area of Naivasha, Kenya

#### 3.1. The Energy Balance Closure Problem

Energy balance is closed when the energy incoming into a system equals the energy outgoing plus any change in energy storage in the system. This is expressed as:

$$R_n = G + H + LE + C \quad 3.1$$

where  $R_n$  is the net radiation,  $G$  is the ground heat flux,  $H$  is the sensible heat flux,  $LE$  is the latent heat flux and  $C$  is the closure or residual term. Following the principle of energy conservation (first law of thermodynamics), the energy balance residual term should be zero (M. Aubinet et al., 1999). However, with many eddy covariance systems, this is not the case. Many studies have reported imbalances of 10-30% (Twine et al., 2000). The problem of lack of energy closure continues to be unresolved and many researchers have tried to evaluate the source of these imbalances. Different studies attribute lack of energy balance closure to: (i) systematic measurement errors, (ii) neglected energy storages, (iii) mismatch in the footprints of turbulent fluxes and the available energy, (iv) advection, and (v) losses through uncaptured high or low frequency contributions to turbulent fluxes (Kidston et al., 2010).

### **3.1.1. Systematic Measurement Errors**

Instrument uncertainty is difficult to quantify given that it is often fused with other multiple factors and thus difficult to single out. Using pairs of instruments from collocated towers, Dragoni et al. (2007) estimated instrument uncertainty of  $\sim 13\%$ . As discussed by Baldocchi et al. (2001), FLUXNET emphasizes the importance of instrument calibration as this can reduce measurement errors. To minimize errors, regular instrument calibration to account for instrument drifts need to be done (Aubinet, Vesala, & Papale, 2012).

### **3.1.2. Neglected Energy Storages**

Including energy storage within the canopy is important when analyzing closures over forests and densely vegetated areas. Wilson et al., (2002) found that including canopy storage improved closure by up to 7% in FLUXNET sites within forests. Including canopy storage in sparsely vegetated areas does not significantly improve closure as this term is very small in such areas. For sparsely vegetated areas like grasslands and farmlands, including soil heat storage term (G) improved closure by up to 20%.

### **3.1.3. Mismatch in the Footprints of Turbulent Fluxes and the Available Energy**

Net radiation and soil heat flux source areas are in order of few metres from the tower, while turbulent fluxes source areas can be hundreds of metres in the upwind direction and as such, there is always a mismatch. Having the turbulent fluxes being measured from a different surface than that of the residual energy measurements is an obvious source of lack of energy balance closure as discussed by Wilson et al. (2002).

### **3.1.4. Advection**

One of the theoretical requirements for eddy covariance measurements is lack of advection. Horizontal advection can however be substantial, especially over heterogeneous areas (Vidale et al., (1997). Lee & Hu (2002) attributed lack of closure during nocturnal periods to advection

## 4. RESEARCH METHODOLOGY

### 4.1. Methodology Flowchart

Figure 4.1 shows a flowchart summarizing the methodology that was adopted in this study.

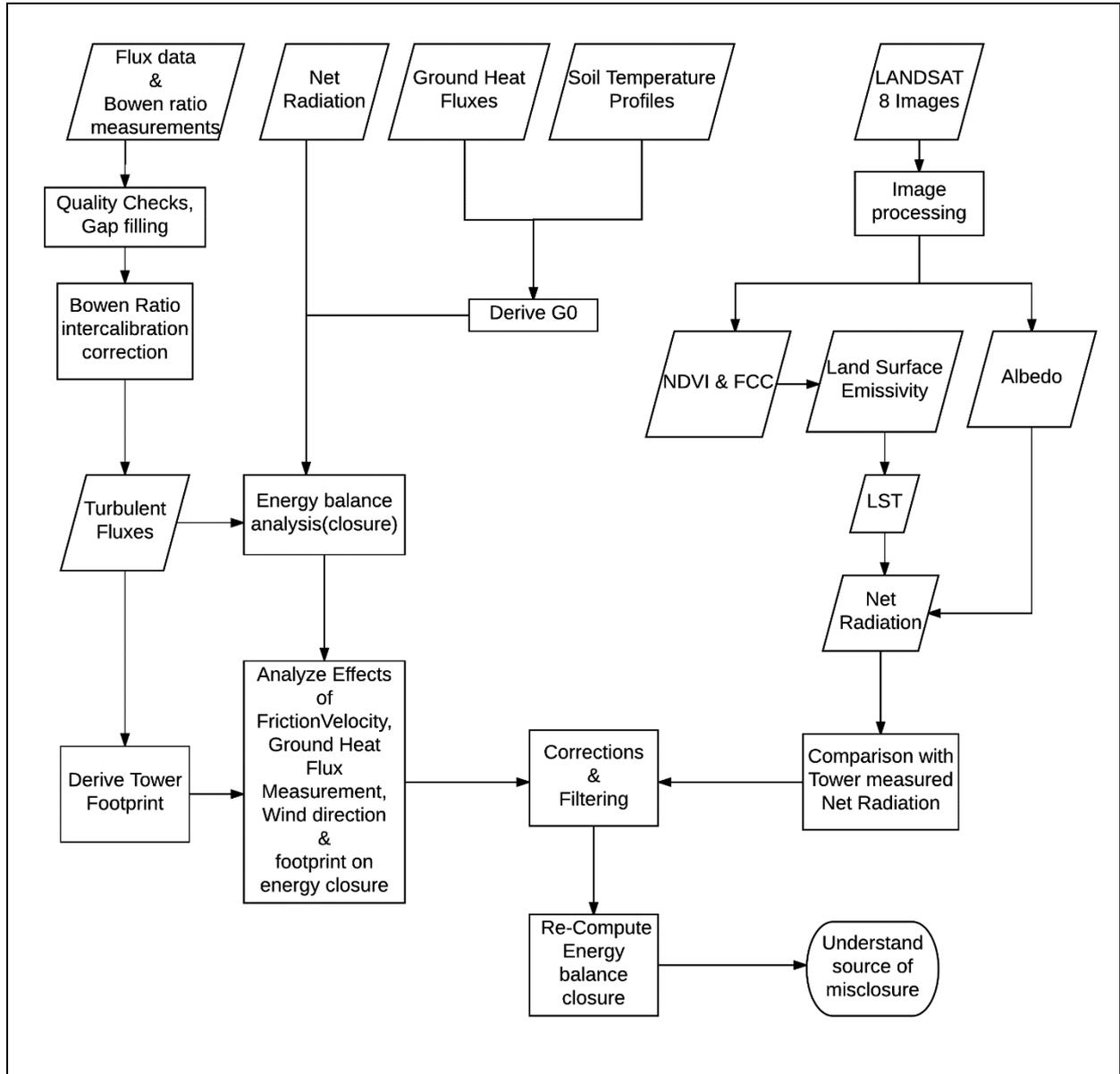


Figure 4.1: Methodology Flowchart

### 4.2. Data Quality Checks

Theoretical requirements for eddy covariance measurements include steady state conditions, fully developed turbulence and horizontal homogeneity. Procedures suggested by Foken et al. (2004) were used to check for fulfilment of steady state and turbulence requirements and data that did not fall within class 1

to 3 in the overall quality flagging classification was flagged out. These flags were implemented in Alteddy 3.9 software used to process turbulent fluxes.

### 4.3. Turbulent Fluxes

Half-hourly averaged turbulent fluxes were processed from the flux measurements using Alteddy software version 3.90 (<http://www.climatexchange.nl/projects/alteddy/>), developed by the Alterra Institute, Wageningen University, The Netherlands. Standard corrections applied during the flux data processing included angle of attack correction following Nakai (2006), 2D axis rotation (Finnigan, 2004), despiking (Vickers & Mart, 1997) and frequency response corrections (Moore, 1986).

Alteddy only processed latent heat fluxes over a short period of time (between 21/03/2012 and 09/05/2012) when the gas analyzer was operational. For the rest of the time series, only sensible heat fluxes were processed, and latent heat fluxes were derived using the Bowen ratio method. The Bowen ratio first proposed by Bowen (1926) is the ratio of sensible heat flux to water vapour flux; and is expressed as:

$$\beta = \frac{H}{LE} = \gamma \frac{\Delta T / \Delta Z}{\Delta e / \Delta Z} \quad 4.1$$

Where  $\gamma$  is the psychrometric constant ( $\text{kPa K}^{-1}$ ),  $\Delta T / \Delta Z$  is the vertical temperature gradient and  $\Delta e / \Delta Z$  is the vertical actual water vapour gradient. Temperature and relative humidity gradients are measured across two fixed heights. Saturated vapour pressure at the two heights was computed using Eq. 4.2 (Buck, 1981).

$$e_s = 6.1121 \exp\left(\left(18.678 - \frac{T}{234.5}\right)\left(\frac{T}{257.14 + T}\right)\right) \quad 4.2$$

Where  $e_s$  is the saturation vapour pressure ( $\text{kPa}$ ) and  $T$  is temperature ( $^{\circ}\text{C}$ ). The relationship between saturated vapour pressure and relative humidity in Eq. 4.3 was used to calculate actual vapour pressure at the two heights enabling computation of  $\Delta e$  from relative humidity RH (expressed as percentage).

$$e = e_s * \frac{RH}{100} \quad 4.3$$

$LE$  was then calculated by inverting the Bowen ratio as shown in Eq. 4.4

$$LE = \frac{H}{\beta} \quad 4.4$$

The Bowen ratio method yields unreasonable fluxes when  $\beta \approx -1$ . This tends to occur during early morning hours, in the afternoon and during precipitation (Ohmura Atsumu, 1982). Fluxes during precipitation and when Bowen ratio approached -1, i.e.  $-1.25 < \beta < -0.75$  were excluded (Payero et al., 2003).

#### 4.4. Inter-calibration of Bowen ratio measuring equipment

As aforementioned, Bowen ratio is calculated using temperature and humidity gradients across two fixed heights. Given that the instruments have been in the field for a long time, there is a possibility of a slight drift which may result in systematic measurement errors (Tomlinson, 1996), thus the need for inter-calibration. Inter-calibration is based on the premise that measurements from two identical equipment under similar conditions should be equal (Tang & Li, 2014). To obtain inter-calibration data, both the Relative Humidity and Temperature (RHT) sensors were mounted at the same height and measurements taken for a period of 5 days, between 19<sup>th</sup> and 23<sup>rd</sup> September 2016. Equations used for inter-calibration correction were obtained by second order polynomial regression of RH<sub>1</sub> against RH<sub>2</sub>, and linear regression of T<sub>1</sub> against T<sub>2</sub>. RHT<sub>2</sub> was chosen as the reference, and the coefficients obtained from the regressions were used to correct RH<sub>1</sub> and T<sub>1</sub> measurements. Figure 4.2 shows regression plots of RHT measurements taken between 19<sup>th</sup> and 23<sup>rd</sup> September 2016 when the sensors were mounted at the same height.

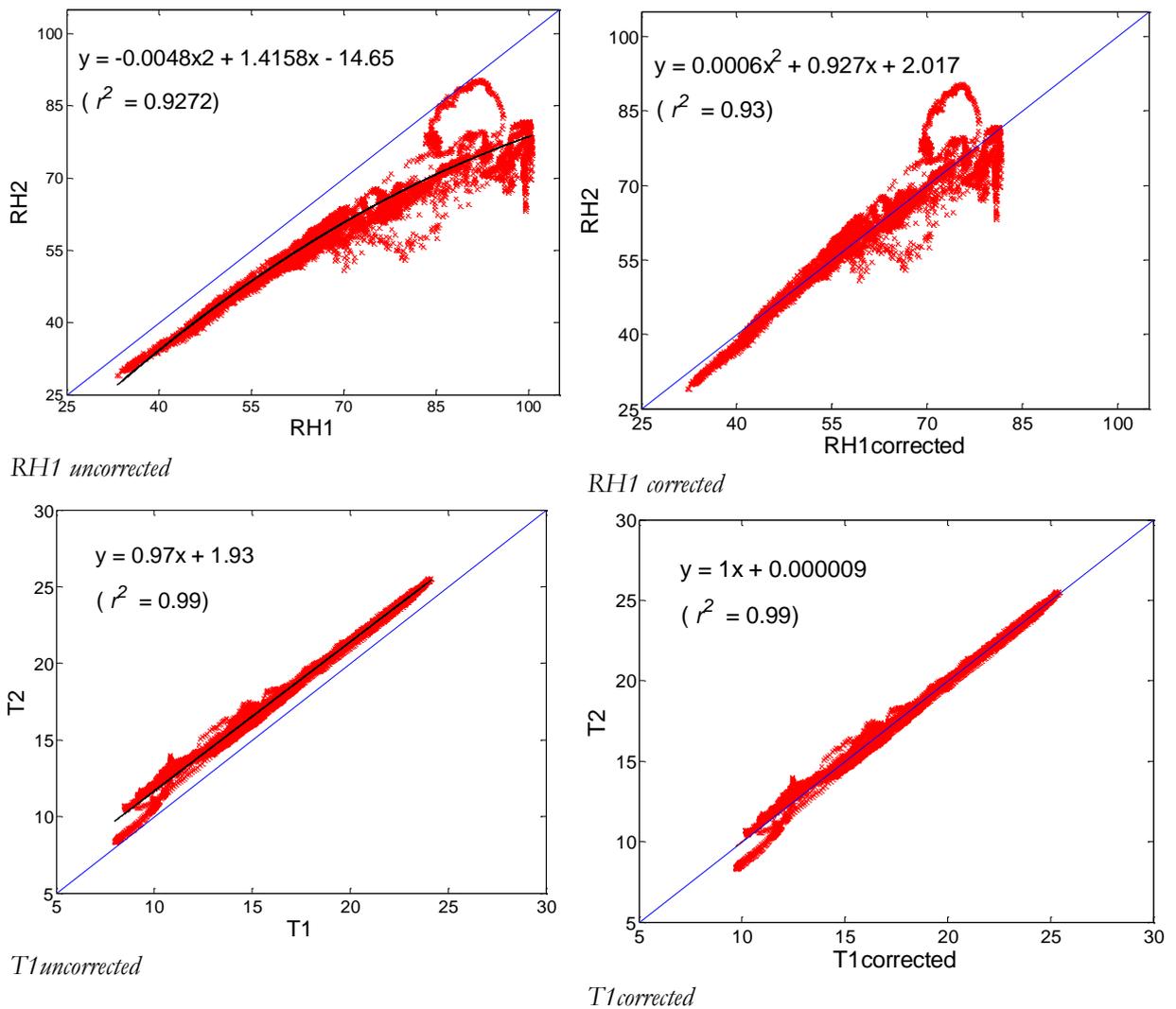


Figure 4.2: Regression plots used to obtain equations used for RH and T inter-calibration correction. The blue line indicates 1:1 relationship.

#### 4.5. Ground Heat Flux

Ground heat flux often receives less attention in comparison with other components of the energy balance, since it is considered the smallest term. Heat absorbed during the day is emitted during the night, and therefore its summation over 24hrs is close to zero (C Van der Tol & Parodi, 2011). For instantaneous energy balance however, ground heat flux accounts for considerable percentage especially in sparsely vegetated areas and savannahs, and as such it cannot be neglected. Ground heat flux at midday for example can range from 30-45% for dense vegetation and bare soil respectively (Heusinkveld et al., (2004); Clothier et al., (1986).

In this study, ground heat flux at the surface was derived using the procedures of Christiaan van der Tol, (2012); which rely on the heat diffusion equation (Eq. 4.5) and the continuity equation for transfer of heat vertically (Eq. 4.6).

$$G(z, t) = -\lambda_s \frac{\partial T(z, t)}{\partial z} \quad 4.5$$

$$c_v \frac{\partial T(z, t)}{\partial t} = -\frac{\partial G(z, t)}{\partial z} \quad 4.6$$

Where  $\lambda_s$  is the thermal conductivity of soil ( $\text{J m}^{-1} \text{s}^{-1} \text{K}^{-1}$ );  $T$  is the soil temperature ( $^{\circ}\text{C}$  or  $\text{K}$ ),  $z$  is the soil depth (m) and  $c_v$  is the volumetric heat capacity ( $\text{J m}^{-1} \text{s}^{-1} \text{K}^{-1}$ ). Combining equation 4.5 and 4.6 gives the thermal diffusion equation (4.7).

$$\frac{\partial T}{\partial t} = D \frac{\partial^2 T}{\partial z^2} \quad 4.7$$

Where  $D = \lambda_s / c_v$  is the soil heat diffusivity ( $\text{m}^2 \text{s}^{-1}$ ). Given that soil heat flux has a periodic nature caused by solar radiation, sinusoidal functions are chosen as boundary conditions to Eq. 4.7. Solving the periodic boundary condition yields eq. 4.8:

$$T(z, t) = \sum_{k=0}^n A_k \sin(\omega kt - Kz) + B_k \cos(\omega kt - Kz) \exp(-Kz) \quad 4.8$$

With this equation, temperature time series at any depth can be simulated analytically. Using Eq. 4.8 in Eq. 4.5 yields an equation for ground heat flux at the surface as a function of temperature:

$$G_0(t) = \Gamma \sum_{k=0}^n \sqrt{k\omega/2} ((A_k - B_k)\sin(\omega kt) + (A_k + B_k) \cos(\omega kt)) \quad 4.9$$

Where  $\Gamma = c_v \cdot \sqrt{D}$  is the thermal inertia of soil ( $\text{J m}^{-2} \text{K}^{-1} \text{s}^{-1/2}$ ). Diffusivity was estimated by calibration of Eq. 4.8 to a measured temperature profile using the least square algorithm 'lsqnonlin' in MATLAB. Using an initial value of  $D$ , temperature time series at all depths is simulated and the squared difference between the measured and simulated temperature is used as objective function for minimisation following procedures by Christiaan van der Tol (2012) . All the analysis were done using MATLAB R2013b.

#### 4.6. Energy Balance Closure

Energy balance closure was evaluated using two methods as discussed by Wilson et al. (2002). One method involves linear regression of the sum of the turbulent fluxes ( $H + LE$ ) against the residual energy ( $R_n - G$ ). The slope and intercept (linear regression coefficients) quantifies the closure. A slope of one and an intercept of zero implies ideal closure. Another method for analysing closure is the Energy balance Ratio (EBR) which involves dividing the sum of turbulent fluxes with the sum of the residual energy as shown in Eq. 4.10.

$$EBR = \frac{\sum(H + LE)}{\sum(R_n - G)} \quad 4.10$$

The advantage of EBR method is that it averages half hourly periods random errors over longer timescales.

#### 4.7. Satellite Data Processing

##### 4.7.1. Atmospheric correction

Atmospheric correction of satellite images was done using Dark Object Subtraction (DOS1) using QGIS software. The location of the study area near a deep water body (L. Naivasha) makes this method suitable. As described by Song et al. (2001), DOS1 method assumes existence of a dark object within the image, which has very low DN values. It is assumed that the minimum DN value is due to an atmospheric effect, and thus it is subtracted from all the pixels. Thermal bands (band 10 and 11) were corrected using the thermal atmospheric correction tool in ENVI software.

##### 4.7.2. DN Conversion to TOA Reflectance and Radiance

Conversion from DN to TOA reflectance for VIS/NIR and radiance for TIR bands was done using equations 4.11, 4.12 and 4.13 as outlined in USGS (2016).

$$L_\lambda = M_L Q_{CAL} + A_L \quad 4.11$$

Where  $L_\lambda$  is the TOA spectral radiance ( $W m^{-2} srad^{-1} \mu m^{-1}$ ),  $M_L$  is the band specific radiance multiplicative factor,  $Q_{CAL}$  is the DN number and  $A_L$  is the band specific radiance additive rescaling factor.

$$\rho\lambda' = M_\rho Q_{CAL} + A_\rho \quad 4.12$$

$$\rho\lambda = \frac{\rho\lambda'}{\cos(\theta_{SZ})} \quad 4.13$$

Where  $\rho\lambda'$  is the TOA planetary reflectance without sun angle correction,  $M_\rho$  is the band specific reflectance rescaling factor,  $A_\rho$  is the reflectance additive rescaling factor  $\rho\lambda$  is the TOA planetary reflectance corrected for sun angle and  $\theta_{SZ}$  is the local solar zenith angle. Rescaling factors and solar zenith angle were obtained from the image metadata files.

##### 4.7.3. Normalized Difference Vegetation Index (NDVI)

NDVI maps were derived from band 4 and band 5 (red and near-infrared bands) of atmospherically corrected images using equation 4.14

$$NDVI = \frac{\rho_5 - \rho_4}{\rho_5 + \rho_4} \quad 4.14$$

Where  $\rho_5$  and  $\rho_4$  are land surface reflectances of band 5 and band 4 respectively.

#### 4.7.4. Fractional Vegetation Cover (FVC)

Fractional vegetation cover (FVC) maps which are required for estimation of land surface emissivity were derived from NDVI using equation 4.15.

$$FVC = \frac{NDVI - NDVI_S}{NDVI_V + NDVI_S} \quad 4.15$$

Where  $NDVI_S$  and  $NDVI_V$  refer to NDVI of soil and NDVI of vegetation respectively. The challenge with this method is determining the NDVI thresholds especially for soil which is characterized by more variation. For this study,  $NDVI_S$  and  $NDVI_V$  were chosen as 0.15 and 0.9 respectively as suggested by Jiménez-Muñoz et al. (2009). FVC was set to zero in pixels with  $NDVI < NDVI_S$  and to one for pixels with  $NDVI > NDVI_V$ .

#### 4.7.5. Land Surface Emissivity (LSE)

Land surface emissivity maps were calculated using simplified NDVI thresholds method proposed by (Sobrino et al. (2008), given by equation 4.16

$$\varepsilon = \begin{cases} \varepsilon_s & NDVI < NDVI_S \\ \varepsilon_s + (\varepsilon_v - \varepsilon_s) * FVC, & NDVI_S \leq NDVI \leq NDVI_V \\ \varepsilon_v & NDVI > NDVI_V \end{cases} \quad 4.16$$

Where  $\varepsilon_s$  refers to emissivity of soil, and  $\varepsilon_v$  is the emissivity of vegetation. Yu, Guo, & Wu (2014) calculated Band 10 emissivity for Landsat 8 TIRS from University of California MODIS emissivity library and obtained values of 0.9668 and 0.9863 for soil and vegetation respectively. These values were adopted for this study.

#### 4.7.1. Albedo

Total shortwave broadband albedo maps were derived using equation 4.17 first proposed by Liang et al. (2003) for Landsat 7 ETM+. The bands were shifted appropriately for its applicability in Landsat 8 OLI.

$$\alpha = 0.356\rho_2 + 0.130\rho_4 + 0.373\rho_5 + 0.085\rho_6 + 0.072\rho_7 - 0.0018 \quad 4.17$$

Where  $\alpha$  is the shortwave broadband albedo, and  $\rho_i$  refers to spectral albedos.

#### 4.7.2. Land Surface Temperature (LST)

USGS has raised concerns about stray light effect on Landsat 8 thermal bands, which is described in Landsat 8 data user handbook (USGS, 2016). They caution users against use of band 11 which appears to be more affected in land surface temperature retrieval algorithms such as the split window algorithm (USGS, 2015). In this study therefore, a generalised single channel algorithm first developed by Jiménez-Muñoz & Sobrino (2003) and revised by Jimenez-Munoz et al. (2009) was used. Only band 10 TIR data was utilised. The general formulation followed in single channel approach is as given in equations 4.18;

$$T_s = \gamma \left[ \frac{1}{\varepsilon} (\varphi_1 L_{sen} + \varphi_2) + \varphi_3 \right] + \delta \quad 4.18$$

Where  $T_s$  is the land surface temperature (LST),  $L_{sen}$  is the at sensor radiance and  $\varepsilon$  is the surface emissivity.  $\gamma$  and  $\delta$  are parameters dependent on the Planck's function calculated using equations 4.19 and 4.20.

$$\gamma \approx \frac{T_{sen}^2}{b_\gamma L_{sen}} \quad 4.19$$

$$\delta \approx T_{sen} - \frac{T_{sen}^2}{b_\gamma} \quad 4.20$$

Where  $T_{sen}$  is at sensor brightness temperature and the parameter  $b_\gamma$  is taken to be 1277K. These parameters are described in detail by Jimenez-Munoz et al. (2009). Parameters  $\varphi_1$ ,  $\varphi_2$  and  $\varphi_3$  represent atmospheric transfer functions (AF's), and are dependent on atmospheric transmissivity, which is determined by water vapour content in the TIR region. They are derived using a matrix notation in equation 4.21.

$$\begin{bmatrix} \varphi_1 \\ \varphi_2 \\ \varphi_3 \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix} \begin{bmatrix} w^2 \\ w \\ 1 \end{bmatrix} \quad 4.21$$

Where  $w$  is the water vapour content and  $C_{ij}$  are coefficients obtained by simulation. In this study, coefficients in Table 4.1; obtained by Jimenez-Munoz et al., (2009) from the TIGR61 database were used.

Table 4.1: Coefficients from TIGR61 database for estimating atmospheric transfer functions (AF's)

| $C_{ij}$ | $i = 1$  | $i = 2$  | $i = 3$  |
|----------|----------|----------|----------|
| $j = 1$  | 0.07593  | -0.07132 | 1.08565  |
| $j = 2$  | -0.61438 | -0.70916 | -0.19379 |
| $j = 3$  | -0.02892 | 1.46051  | -0.43199 |

Total column water vapour content estimates ( $w$ ) were obtained from ECMWF. Retrieved water vapour values together with calculated AF's are shown in Table 4.2. Sample maps of LST derived using the single channel algorithm are shown in Appendix A.

#### 4.7.3. Net Radiation

Net radiation maps were calculated using equation 4.22

$$R_n = (1 - \alpha)R_{si} + R_{li} - R_{lo} \quad 4.22$$

Where  $R_n$  is the net radiation,  $\alpha$  is broadband shortwave albedo (from albedo maps),  $R_{si}$  is the incoming shortwave radiation,  $R_{li}$  is the incoming longwave radiation and  $R_{lo}$  is the outgoing longwave radiation.  $R_{lo}$  maps were calculated using equation 4.23.

$$R_{lo} = (1 - \varepsilon)R_{li} + \varepsilon\sigma T_0^4 \quad 4.23$$

Where  $\sigma$  is the Stefan Boltzmann constant ( $5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-1}$ ),  $\varepsilon$  is the emissivity (from emissivity maps) and  $T_0$  is the land surface temperature in Kelvin (from LST maps). Given that emissivity maps were

used for LST maps retrieval, any errors in the emissivity estimation are compensated for in the calculation of broadband outgoing albedo in eq. 4.23.  $R_{si}$  and  $R_{li}$  values were obtained from the ground measurements at the flux tower corresponding to the satellite overpass time. ILWIS software map calculation was extensively used in implementing the formulations used to calculate NDVI, FVC, LSE, albedo, LST and net radiation maps. Net radiation measured at the tower was compared with net radiation derived from the satellite both at the tower pixel and when averaged within the tower footprint. Sample maps of LST derived using the single channel algorithm are shown in Appendix A. Net radiation maps are shown in Appendix B.

Table 4.2: Total column water vapour estimates retrieved from ECMWF: <http://apps.ecmwf.int/datasets/data/interim-full-daily/levtype=sfc/>, and calculated AF's.

| Date       | Total column Water                      |   |
|------------|---|---|
|            | Vapour estimate<br>[g/cm <sup>2</sup> ] | $\varphi_1$ , $\varphi_2$ and $\varphi_3$                           |
| 17/07/2013 | 1.5249                                  | $\varphi_1$ 1.07550<br>$\varphi_2$ -0.33652<br>$\varphi_3$ -0.17758 |
| 05/10/2013 | 1.5012                                  | $\varphi_1$ 1.07631<br>$\varphi_2$ -0.32045<br>$\varphi_3$ -0.20311 |
| 22/11/2013 | 2.009                                   | $\varphi_1$ 1.07465<br>$\varphi_2$ -0.35496<br>$\varphi_3$ -0.14901 |
| 24/12/2013 | 1.4607                                  | $\varphi_1$ 1.07675<br>$\varphi_2$ -0.31238<br>$\varphi_3$ -0.21618 |
| 25/01/2014 | 1.5734                                  | $\varphi_1$ 1.07697<br>$\varphi_2$ -0.30838<br>$\varphi_3$ -0.22271 |
| 26/02/2014 | 1.7065                                  | $\varphi_1$ 1.07750<br>$\varphi_2$ -0.29915<br>$\varphi_3$ -0.23796 |
| 30/03/2014 | 1.2977                                  | $\varphi_1$ 1.07471<br>$\varphi_2$ -0.35354<br>$\varphi_3$ -0.15119 |
| 17/05/2014 | 1.54046                                 | $\varphi_1$ 1.07560<br>$\varphi_2$ -0.33449<br>$\varphi_3$ -0.18077 |
| 02/06/2014 | 2.3522                                  | $\varphi_1$ 1.07369<br>$\varphi_2$ -0.37807<br>$\varphi_3$ -0.11425 |
| 04/07/2017 | 1.5399                                  | $\varphi_1$ 1.07646<br>$\varphi_2$ -0.31766<br>$\varphi_3$ -0.20761 |
| 21/08/2014 | 1.4263                                  | $\varphi_1$ 1.07562<br>$\varphi_2$ -0.33403<br>$\varphi_3$ -0.18149 |

#### **4.8. Flux footprint**

Flux footprint refers to the contribution of the upwind elements to fluxes measured at a point (Kim et al., 2006). Vesala et al. (2008) illustratively defines it as ‘the field of view of the flux sensor’. An obvious cause of lack of energy balance closure as discussed by Wilson et al. (2002) is having the turbulent fluxes being measured from a different surface than that of the residual energy measurements. Knowing the turbulent fluxes source area can aid in understanding whether this is the case.

Over the past few decades, several footprint functions describing flux source areas have been developed. In this study, flux footprints were calculated using the Flux Footprint prediction (FFP) model by Kljun et al. (2015). FFP is a 2-dimensional parameterized footprint model, based on the 3-D backward Lagrangian stochastic particle dispersion model by Kljun, Rotach, & Schmid (2001). Unlike previous models, it makes it possible for evaluation of long time series data owing to its low computational demand. Apart from enabling calculation of single footprints, FFP allows calculation of climatology foot print from half hourly time step series. Aggregated climatology footprints were calculated for years 2012, 2013 and 2014. Single footprints were also derived during peak radiation at noon. For visualisation of extends on the study area, footprints were overlaid on a Google Earth image. The FFP MATLAB code used was downloaded from <http://footprint.kljun.net/>.



## 5. RESULTS AND DISCUSSION

### 5.1. Diurnal Variation of Fluxes

Figure 5.1 shows diurnal variations of flux partitions during the year 2012.

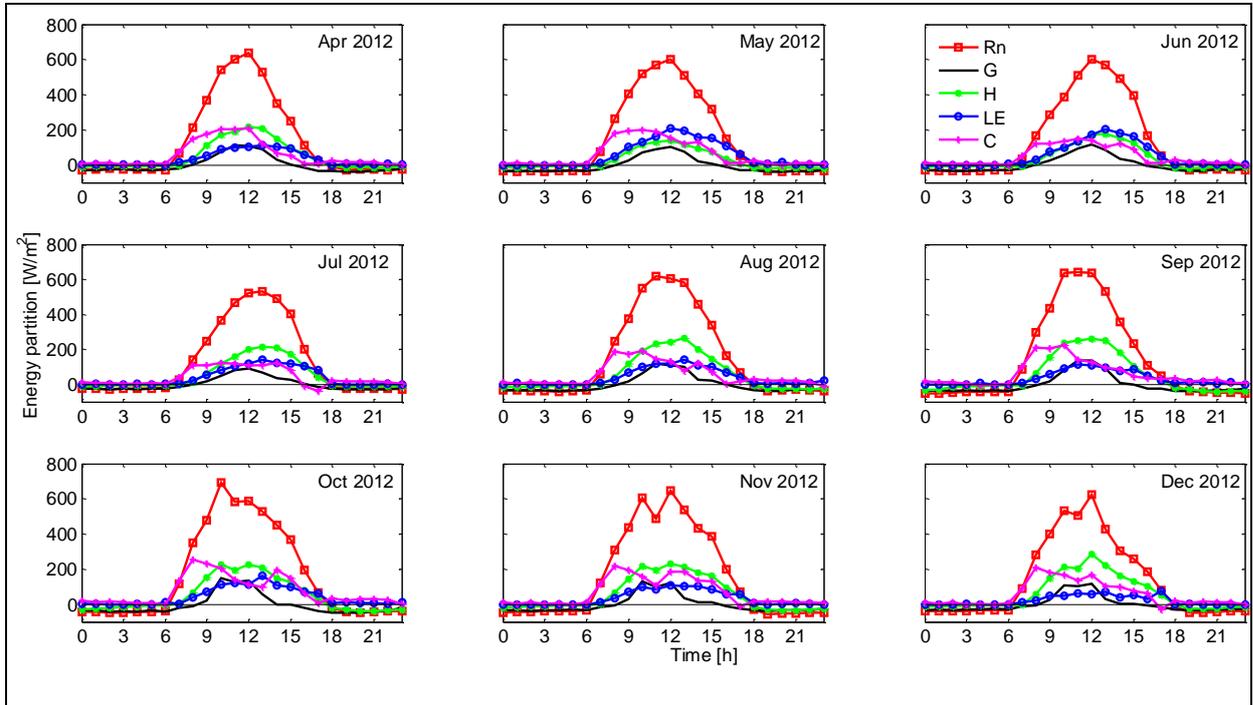


Figure 5.1: Hourly averaged fluxes showing diurnal flux variations in the year 2012. The closure term is shown in purple.

Net radiation peaks at 600-700  $\text{W m}^{-2}$ , with slight variations over the months. As expected the peak occurs at midday. Sensible and latent heat show more variability; and even though sensible heat is generally higher than latent heat in most of the months, in May and June latent heat is higher than sensible heat. This is due to increased water availability following the rain season, thus increased evapotranspiration. After the rainy season, sensible heat becomes more dominant. Odongo et al. (2016) reported similar trends. Ground heat flux is the smallest of all fluxes and just as the sensible and latent heat, it peaks around midday, then gradually reduces over the evening, sometimes going to negative in the night. Table 5.1 shows a summary of monthly averaged energy partitions for the period between 2012 and 2014.

Table 5.1: Monthly averaged energy partitions for the period between 2012 and 2014. Closure term(C) is also shown

| Year | Month | Rn<br>[W/m-2] | G0<br>[W/m-2] | H<br>[W/m-2] | LE<br>[W/m-2] | C<br>[W/m-2] | P<br>[mm] |
|------|-------|---------------|---------------|--------------|---------------|--------------|-----------|
| 2012 | Apr   | 141.10        | 0.50          | 45.80        | 31.89         | 62.91        | 6.08      |
|      | May   | 138.76        | -4.50         | 39.90        | 34.41         | 68.95        | 3.78      |
|      | Jun   | 134.66        | -0.14         | 40.91        | 37.47         | 56.41        | 0.62      |
|      | Jul   | 130.80        | 0.02          | 46.34        | 37.08         | 47.37        | 1.78      |
|      | Aug   | 153.41        | 0.10          | 53.11        | 32.81         | 67.39        | 2.83      |
|      | Sept  | 150.21        | 0.22          | 56.57        | 33.23         | 60.18        | 2.78      |
|      | Oct   | 167.76        | 0.13          | 50.26        | 32.22         | 85.16        | 4.18      |
|      | Nov   | 153.99        | 0.10          | 51.92        | 33.59         | 68.37        | 1.42      |
|      | Dec   | 139.71        | 0.14          | 53.84        | 24.64         | 61.08        | 2.18      |
| 2013 | Jan   | 182.23        | -0.76         | 50.40        | 33.08         | 99.51        | 3.34      |
|      | Feb   | 174.84        | 0.65          | 51.31        | 26.60         | 96.29        | 0.53      |
|      | March | 157.42        | 0.42          | 51.53        | 26.59         | 78.89        | 6.4       |
|      | Apr   | 150.14        | 0.09          | 51.31        | 26.60         | 72.15        | 7.98      |
|      | May   | 157.51        | 0.07          | 51.27        | 26.59         | 79.58        | 1.67      |
|      | Jun   | 142.30        | 0.11          | 46.05        | 31.32         | 64.82        | 1.68      |
|      | Jul   | 154.68        | 0.03          | 56.25        | 23.55         | 74.85        | 2         |
|      | Aug   | 133.42        | -0.46         | 51.10        | 18.71         | 64.07        | 3.13      |
|      | Sep   | 149.81        | 0.93          | 48.68        | 32.31         | 67.90        | 0.25      |
|      | Oct   | 172.42        | 0.13          | 54.38        | 21.45         | 96.46        | 0.96      |
|      | Nov   | 155.03        | 0.25          | 44.47        | 23.29         | 87.02        | 3.39      |
|      | Dec   | 148.57        | -0.13         | 45.87        | 16.83         | 86.00        | 2.98      |
| 2014 | Jan   | 176.62        | 0.38          | 67.26        | 20.16         | 88.82        | 1         |
|      | Feb   | 158.39        | 0.10          | 57.14        | 21.81         | 79.35        | 3.26      |
|      | March | 192.66        | 0.27          | 56.13        | 27.50         | 108.76       | 0.81      |
|      | Apr   | 161.95        | 0.17          | 54.43        | 21.81         | 85.54        | 2.31      |
|      | May   | 141.58        | 0.24          | 53.99        | 22.74         | 64.60        | 1.27      |
|      | Jun   | 138.75        | -0.07         | 53.96        | 19.52         | 65.34        | 1.61      |
|      | Jul   | 144.03        | -0.39         | 56.18        | 27.51         | 60.73        | 3.12      |
|      | Aug   | 148.93        | 0.41          | 51.10        | 27.31         | 70.12        | 2.32      |
|      | Sept  | 165.89        | 0.03          | 48.11        | 25.33         | 92.42        | 3.08      |
|      | Oct   | 154.07        | 0.13          | 50.63        | 23.62         | 79.68        | 1.54      |
|      | Nov   | 138.60        | -0.29         | 51.05        | 15.98         | 71.87        | 2.15      |
|      | Dec   | 157.45        | -4.99         | 51.62        | 26.62         | 84.20        | 1.72      |

## 5.2. Energy Balance Closure

The energy balance ratio (EBR) analysed using data set filtered following Foken et al. (2004) was 67% for 2012, 56% for 2013 and 51% for 2014, with an overall EBR of 58% for the three year period (2012-2014). Slopes of linear regression of H+LE vs Rn-G were 0.72 for 2012, 0.60 for 2013 and 0.57 for 2014, with an overall slope of 0.63 for the three years as shown by the plots on Figure 5.2. The coefficient of determination ( $R^2$ ) ranged between 0.63 and 0.78 while the RMSE ranged between 51.23 and 98.63  $W m^{-2}$ . Energy balance closure analysis was also done for a brief period of 2016 (April 4<sup>th</sup> – June 3<sup>rd</sup>) when the sonic anemometer was working. The slope of linear regression for the 2 months evaluated in 2016 was 0.56, while the EBR was 0.49. The regression coefficients of H+LE vs Rn-G are summarized in Table 5.2.

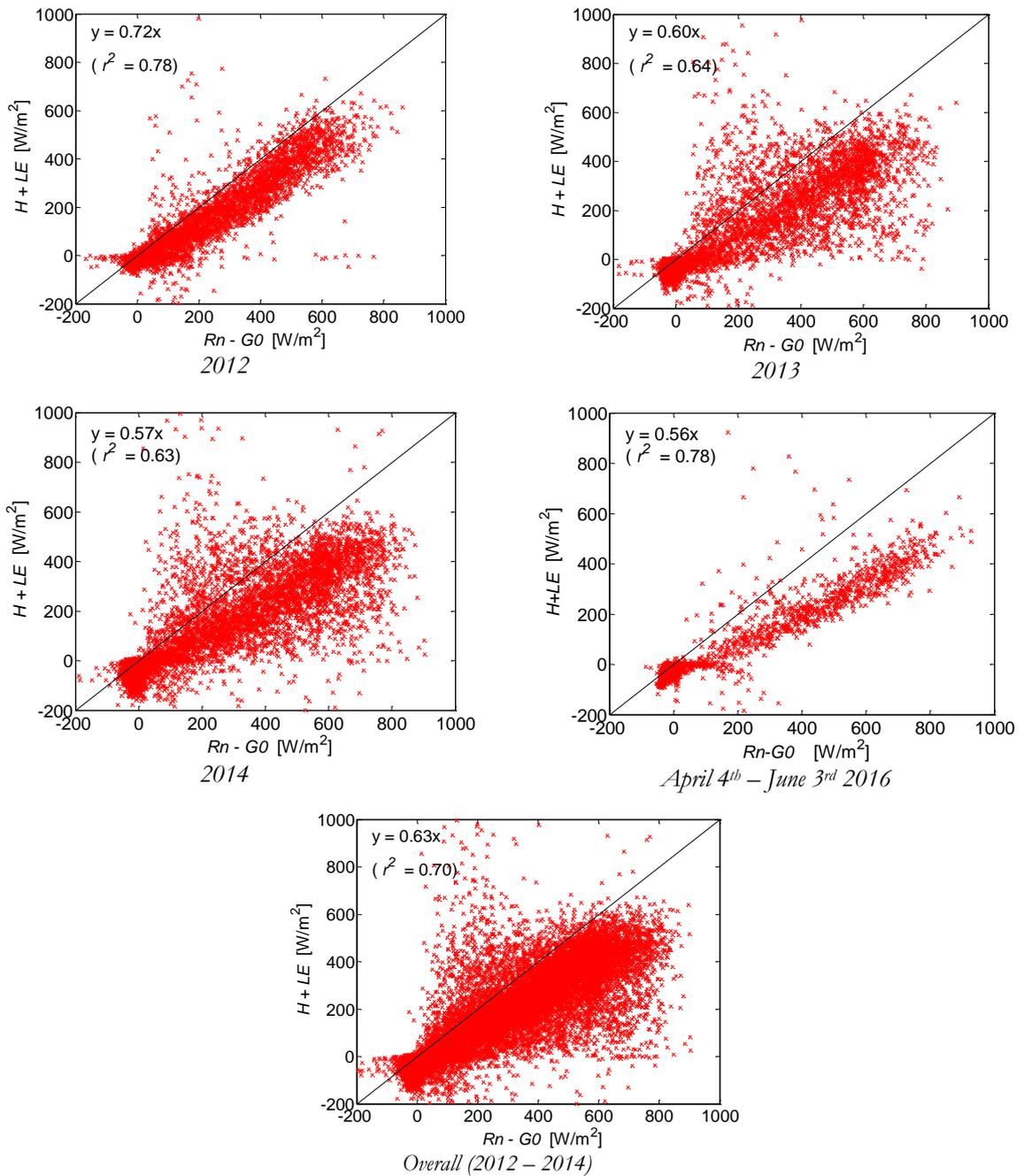


Figure 5.2: Linear regressions of  $Rn-G_0$  vs  $H+LE$  for 2012 – 2014 and April 4<sup>th</sup> – June 3<sup>rd</sup> 2016. Regression lines have been forced through the origin

Table 5.2: Summary of regression coefficients of  $Rn-G_0$  vs  $H+LE$ , EBRs and RMSEs for 2012 – 2014 and April 4<sup>th</sup> – June 3<sup>rd</sup> 2016

|  | Year                       | Slope       | EBR         | RMSE<br>[W m <sup>-2</sup> ] | R <sup>2</sup> |
|--|----------------------------|-------------|-------------|------------------------------|----------------|
| Original data set<br>with Foken et al. (2004)<br>quality flags | 2012                       | 0.73        | 0.67        | 51.23                        | 0.83           |
|  | 2013                       | 0.60        | 0.56        | 98.63                        | 0.64           |
|  | 2014                       | 0.57        | 0.51        | 94.01                        | 0.63           |
|  | 2016 (2 months)            | 0.56        | 0.49        | 61.10                        | 0.78           |
|  | <b>Overall (2012-2014)</b> | <b>0.63</b> | <b>0.58</b> | <b>85.61</b>                 | <b>0.70</b>    |

It appeared that there was systematic reduction in EBR which reduced from 67% to 56%, 51% and 49% for 2012, 2013, 2014 and the two months evaluated in 2016 respectively. Slopes of linear regression of half hourly turbulent fluxes against the residual energy showed a similar reduction from 73% to 60%, 57% and 56% for 2012, 2013, 2014 and the two months evaluated in 2016 respectively. This could have been caused by drifts and systematic errors in the Bowen ratio measurement equipment.

### 5.2.1. Effect of Bowen Ratio Inter-calibration on Energy Balance closure.

Figure 5.3 shows a plot of linear regression of turbulent fluxes against the residual energy for the period between April 4<sup>th</sup> and June 3<sup>rd</sup> 2016 after the Bowen ratio inter-calibration.

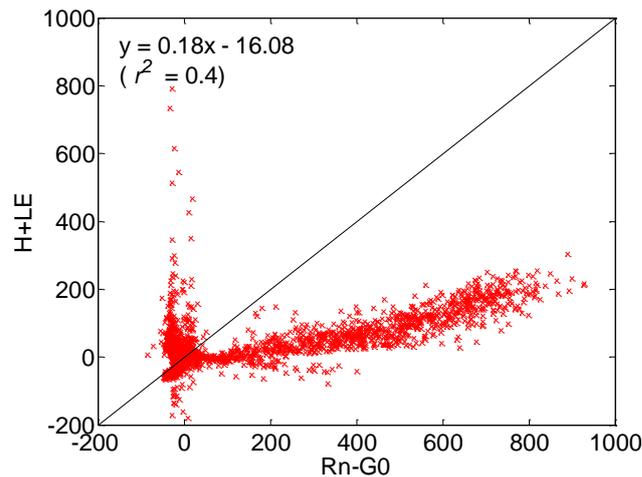


Figure 5.3: 2016 (April 4<sup>th</sup>-June 3<sup>rd</sup>) after Bowen ratio intercalibration

Inter-calibration did not improve the energy balance closure as it had been hypothesized. On the contrary, it deteriorated the closure to an unexpected value of 18% for measurements taken between April 4<sup>th</sup> and June 3<sup>rd</sup> 2016. A technical failure of the sensor aspirators during the inter-calibration period may have led to lack of reliable measurements.

### 5.2.2. Effects of Friction Velocity ( $u^*$ [ $\text{ms}^{-1}$ ]) on the Energy Balance Closure

One of the conditions for the eddy covariance theory is fully developed turbulence. Low values of  $u^*$  [ $\text{ms}^{-1}$ ] are associated with under-developed turbulence. Different authors have applied filtering of low quality data based on a friction velocity threshold (Barr et al., 2013; Nordbo et al., 2012). By filtering out fluxes when  $u^*$  was less than  $0.25 \text{ m s}^{-1}$ , Sánchez et al. (2010) reported an increase of 13% in the EBR. A filtering threshold of  $u^* < 0.3 \text{ m s}^{-1}$  applied by Oliphant et al. (2004) was used in this study. After this filtering, the overall EBR for the three year period (2012-2014) improved by 5% while the yearly EBR's improved by 5% for 2012, 9% for 2013 and 5% for 2014. The overall slope of linear regression improved by 3% while yearly slopes increased by 2% for 2012, 2% for 2013, and 4% for 2014. Closures obtained after applying this filtering were similar to those of Odongo et al. (2016) who reported an overall slope of 0.66 and an EBR of 0.65 for the three years. Table 5.3 summarises the results after filtering data when  $u^*$  was less than  $0.3 \text{ m s}^{-1}$ .

Table 5.3: Summary of Slopes of linear regression of  $R_n - G_0$  vs  $H + LE$ , EBRs and RMSEs after filtering fluxes when  $u^* < 0.3 \text{ m s}^{-1}$

|   | Year                       | Slope | EBR  | RMSE<br>[ $\text{W m}^{-2}$ ] | $R^2$ |
|---|----------------------------|-------|------|-------------------------------|-------|
| <b>Original data set<br/>with Foken et al. (2004)<br/>quality filters</b> | 2012                       | 0.73  | 0.67 | 51.23                         | 0.83  |
|   | 2013                       | 0.60  | 0.56 | 98.63                         | 0.64  |
|   | 2014                       | 0.57  | 0.51 | 94.01                         | 0.63  |
|   | 2016 (2 months)            | 0.56  | 0.49 | 61.10                         | 0.78  |
|   | <b>Overall (2012-2014)</b> | 0.63  | 0.58 | 85.61                         | 0.70  |
| <b>After filtering <math>u^* &lt; 0.3 \text{ m s}^{-1}</math></b>         | 2012                       | 0.75  | 0.72 | 54.65                         | 0.83  |
|   | 2013                       | 0.62  | 0.65 | 124.04                        | 0.62  |
|   | 2014                       | 0.61  | 0.56 | 119.75                        | 0.60  |
|   | 2016 (2 months)            | 0.58  | 0.54 | 70.99                         | 0.72  |
|   | <b>Overall (2012-2014)</b> | 0.66  | 0.63 | 108.06                        | 0.67  |

### 5.2.3. Effects of the Flux Footprint on the Energy Balance Closure

Flux footprint is defined as the contribution of the upwind elements to fluxes measured at a point. Figure 5.4 is a wind rose, showing the prevailing directions in the study area for the periods between 2012 and 2014.

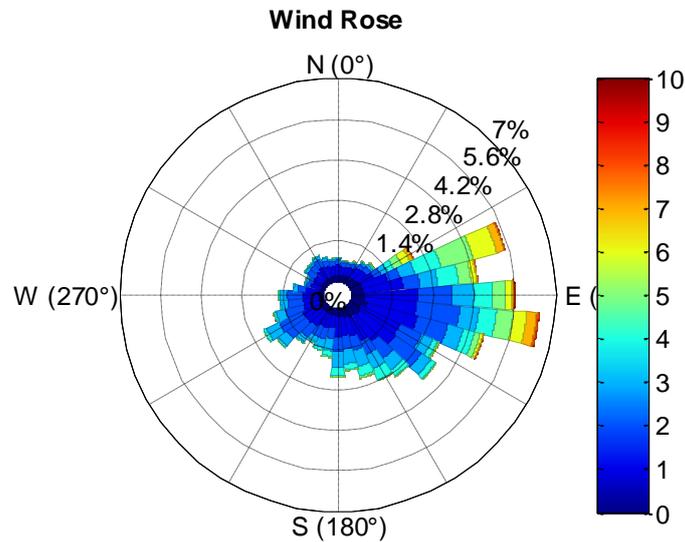


Figure 5.4: Rose diagram showing wind direction for period between 2012 and 2014. The colour bar indicates wind speeds ( $\text{m s}^{-1}$ )

The prevailing wind direction is from from the ESE. Most average wind speeds were up to  $5 \text{ m s}^{-1}$  with a few instances of wind speeds above  $6 \text{ m s}^{-1}$ . Figure 5.5 and Figure 5.6 shows flux footprints derived using the FFP model.

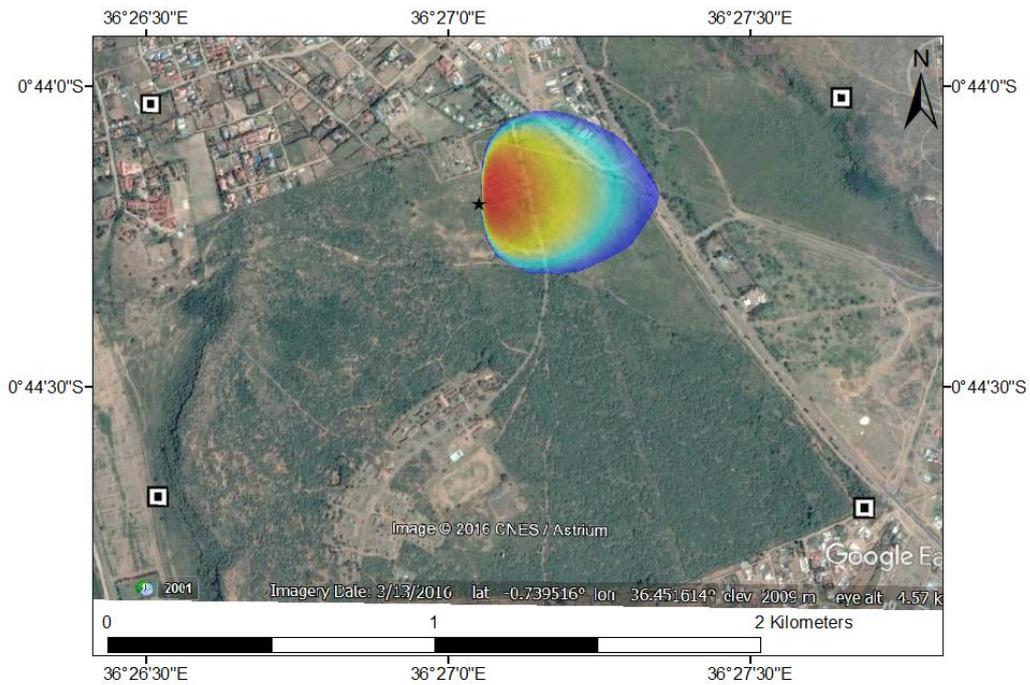


Figure 5.5: Midday flux footprint for 17/07/2013 overlaid on a true colour Google Earth image. The red intensity colour shows the highest contribution area, followed by the yellow, the cyan and the purple. The tower location is shown with a star.

During midday unstable condition (Figure 5.5), the footprint extends eastwards from the tower.

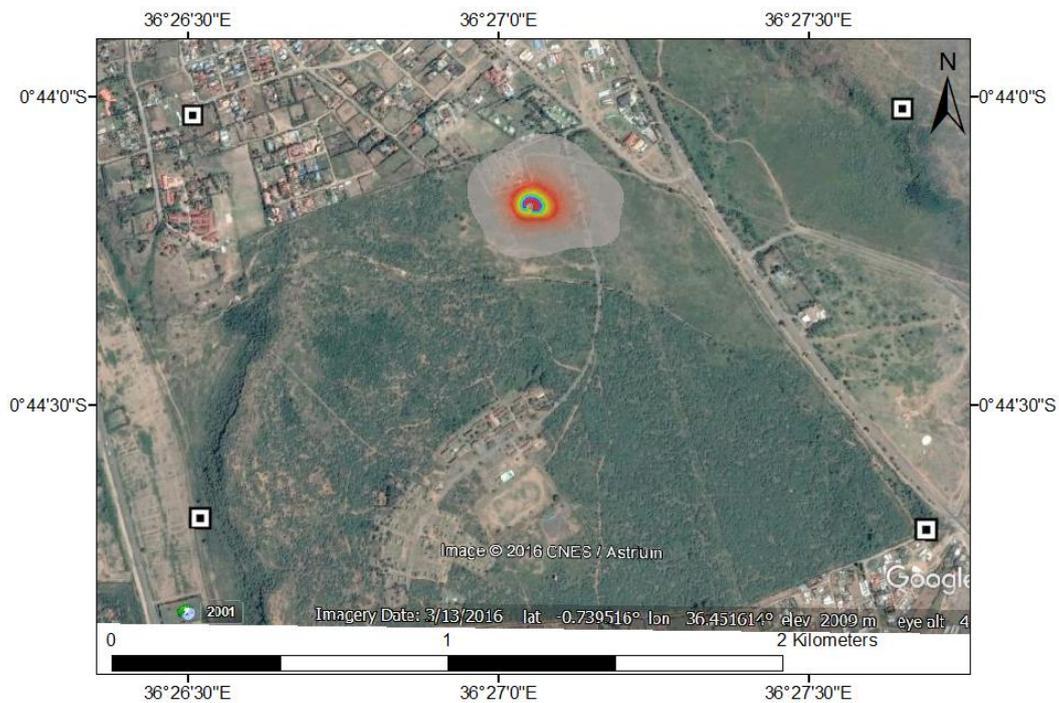


Figure 5.6: Three year climatology footprint (2012-2014). The middle high intensity colour represents highest contribution area. The contribution area reduces with decreasing colour intensity.

From the dimensions of the footprints, it is visible that most of the turbulent fluxes are from the same land cover as the residual fluxes. Some turbulent fluxes are however picked from across the road north eastwards of the tower location. Figure 5.7 shows polar plots of EBR with wind direction (a) as well as the footprint distance vs the wind direction (b).

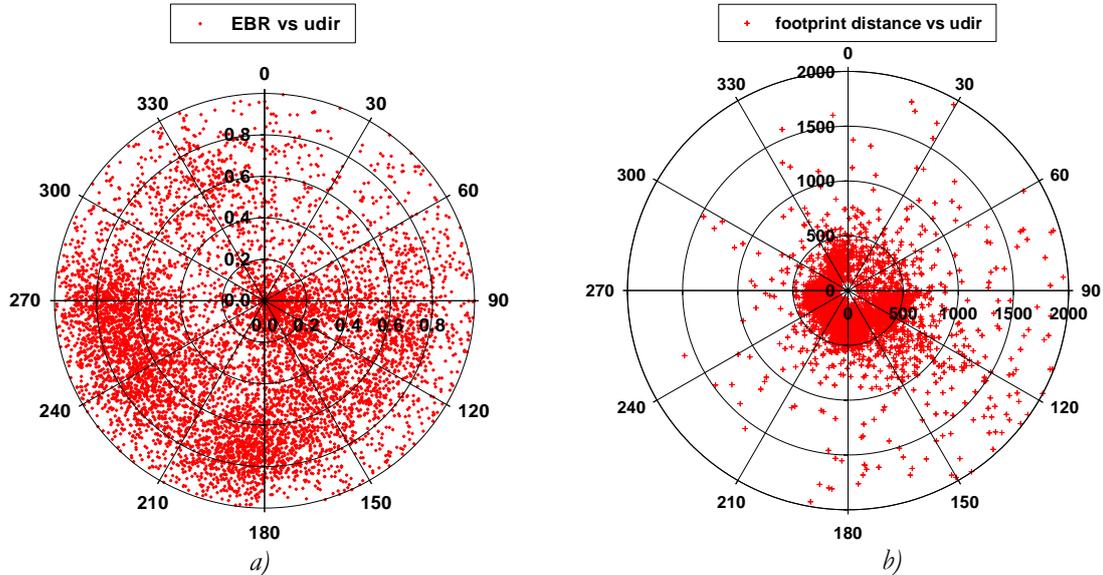


Figure 5.7: Polar plot of EBR vs Wind direction for the period between 2012 and 2014.

Figure 5.7 b shows that most of the footprint source areas are within 500metres from the tower, with a few instances stretching beyond that especially when wind directions are between 60°- 180°. As seen in Figure 5.7 (a), a higher concentration of low values of EBR are observed between 60°- 150° degrees, and this could most likely be attributed to some fluxes emanating from the road surface to the East beyond the savannah in this quadrant. By filtering fluxes emanating from a bare land surface different from the forested area being investigated, Sánchez et al., (2010) found that EBR values improved by 5%. In this study fluxes when wind direction was between 60°-150° were filtered, as they were considered to include the road surface. This increased the overall EBR for the three years (2012-2014) by 6% and yearly EBR's by 5%, 6% and 7% for 2012, 2013 and 2014 respectively. Table 5.4 summarises the coefficients of linear regression of Rn-G0 vs H+LE, the EBRs and RMSEs after filtering fluxes when wind direction was between 60° and 150°.

Table 5.4: Summary of Slopes of linear regression, EBRs and RMSEs after filtering fluxes when wind direction was between 60° and 150°

|  | Year                       | Slope | EBR  | Mean Error<br>[W m <sup>-2</sup> ] | R <sup>2</sup> |
|--|----------------------------|-------|------|------------------------------------|----------------|
| <b>Original data set<br/>with Foken et al. (2004)<br/>quality filters</b>        | 2012                       | 0.73  | 0.67 | 51.23                              | 0.83           |
|  | 2013                       | 0.60  | 0.56 | 98.63                              | 0.64           |
|  | 2014                       | 0.57  | 0.51 | 94.01                              | 0.63           |
|  | 2016 (2 months)            | 0.56  | 0.49 | 61.10                              | 0.78           |
|  | <b>Overall (2012-2014)</b> | 0.63  | 0.58 | 85.61                              | 0.70           |
| <b>After filtering fluxes when<br/>wind direction was<br/>between 60° - 120°</b> | 2012                       | 0.74  | 0.72 | 57.31                              | 0.83           |
|  | 2013                       | 0.60  | 0.62 | 115.92                             | 0.65           |
|  | 2014                       | 0.58  | 0.58 | 101.47                             | 0.69           |
|  | 2016 (2 months)            | 0.52  | 0.55 | 71.68                              | 0.73           |
|  | <b>Overall (2012-2014)</b> | 0.64  | 0.64 | 95.07                              | 0.73           |

**5.2.4. Accuracy in Ground Heat Flux Estimation.**

Due to varying vegetation cover, topography and soil characteristics; representativeness of measured ground heat flux in heterogeneous areas becomes a challenge (Kustas et al., 2000). To obtain more representative measurements, many researchers use averaged measurements from two to nine soil heat flux plates (Stannard et al., 1994; Dugas et al., 1995). Stannard et al. (1994) reported an error of between 30 to 40 W m<sup>-2</sup> in a semi-arid area while comparing measurements from different plates. While using a system of three sensors Kustas et al. (2000) reported deviations of up to 100 W m<sup>-2</sup>. Figure 5.8 shows a plot of ground heat fluxes derived using the four additional soil heat flux plates installed during the fieldwork, together with ground heat flux derived from measurements by a plate to the South which has been taking measurements from 2012. Table 5.5 shows the standard deviation of Ground heat flux measurements from the four additional plates in comparison with the plate to the south

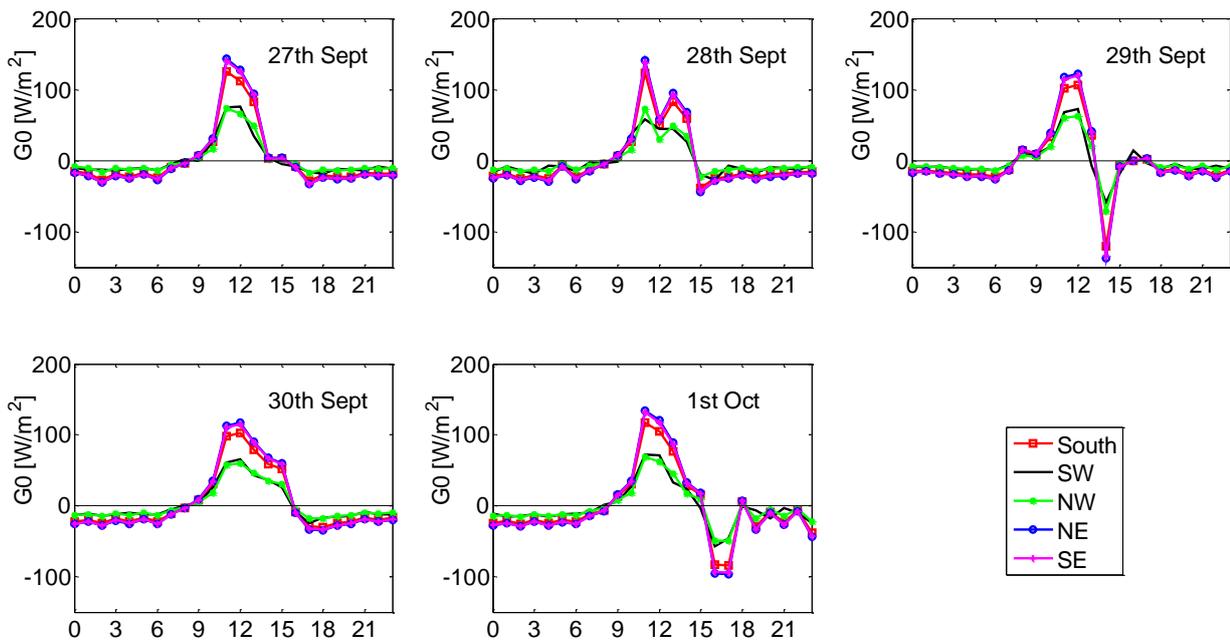


Figure 5.8: Comparison of G derived using measurements from soil heat flux plates installed in different directions (Note: South plate is at 10cm while all others are at 5cm)

Table 5.5: Standard deviation of Ground heat flux measurements from the four additional plates in comparison with the plate to the south.

|  | SE   | NE   | NW    | SW    |
|--|------|------|-------|-------|
| <b>Standard Deviation (W m<sup>-2</sup>)</b> | 9.67 | 9.98 | 18.06 | 19.49 |

When compared to the south plate, ground heat fluxes derived from the west have a higher standard deviation than those from the east as shown in Table 5.5. Estimations from plates towards the west of the tower (SW and NW) show similarity, while those from the east and south of the tower show similarity as well. It should be noted that soil temperature profiles are only measured near the plate to the South and diffusivity estimated from these soil temperature profiles is assumed to be similar for all other directions. This assumption may not be correct, given that the soil thermal properties could be different for the different soil heat flux plate locations. Taking this into account, the variations could be different.

Considering the variability indicated by these measurements, there is a possibility of an error in ground heat flux when it is measured from one point and assumed to be representative of the whole area. Errors in estimation of ground heat flux can be up to 40% (Sánchez et al., 2010). Analysis of the energy balance closure using ground heat flux measurements in the different directions was not possible since the sonic anemometer was not working during the fieldwork period of this study.

### 5.2.5. Representativeness of Net Radiation Measurements and its Effect on Energy Balance Closure

As discussed in Section 3.1.3, mismatch in footprint of net radiation and turbulent fluxes is a possible cause of lack of energy balance closure. Net radiation at the flux tower is measured by a net radiometer, mounted at 2.5 m above the ground. Compared to Landsat 8 OLI & TIRS satellite, the radiometer's field of view is relatively smaller in order of hundreds of  $m^2$ . Figure 5.9 shows two sample maps of net radiation derived from Landsat 8.

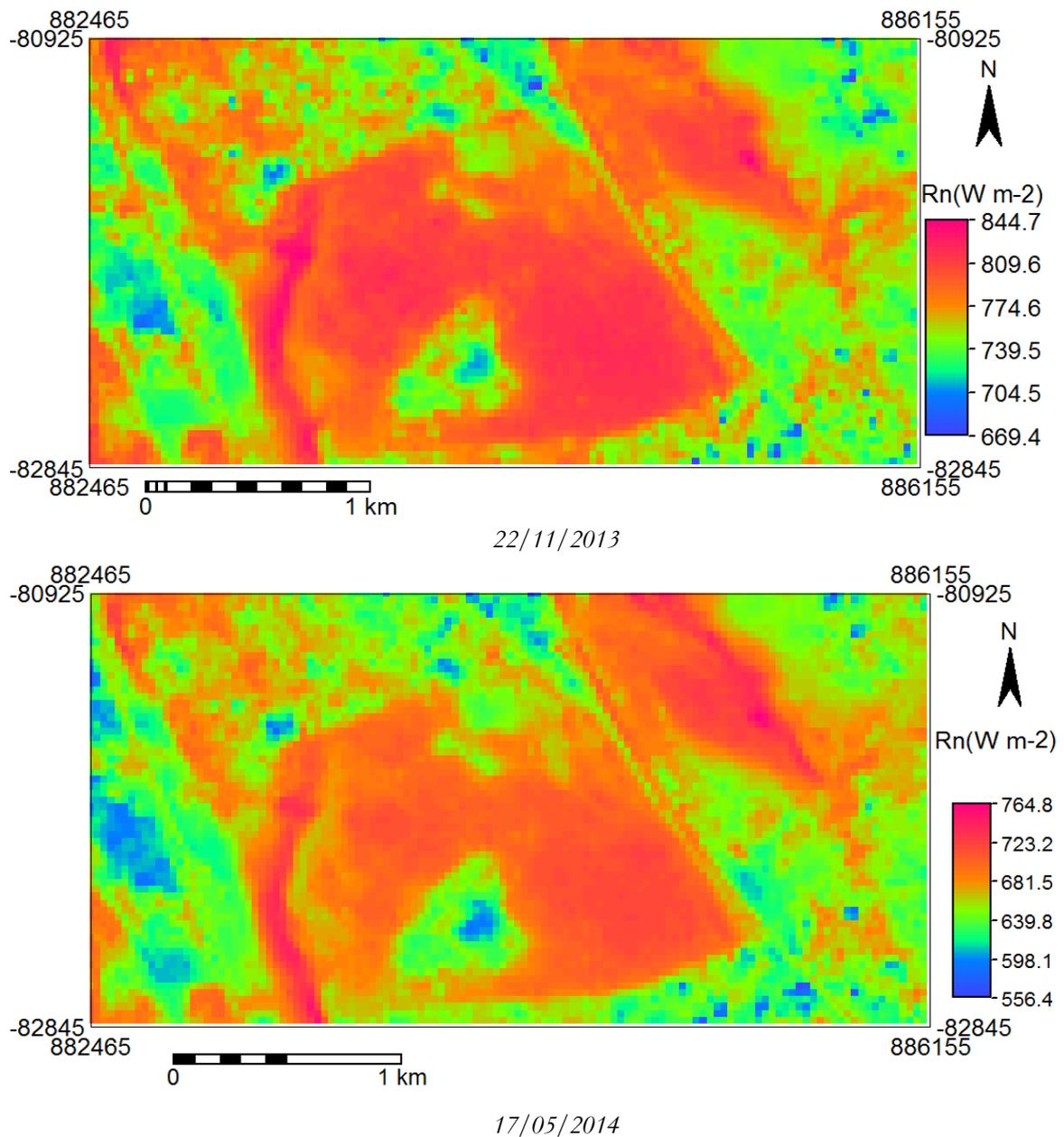


Figure 5.9: Net radiation maps derived from Landsat 8 OLI & TIRS for 22/11/2013 and 17/05/2014. The maps show spatial variability in net radiation over the study area.

Net radiation varies spatially over the study area. As shown in Section 5.2.3, the turbulent fluxes source area (the tower footprint) extends up to several hundred metres from the tower. However, net radiation measured at the tower location is assumed to be equal to net radiation over the turbulent fluxes source area; which is not the case shown by the net radiation maps. Net radiation measured by the tower radiometer was compared with net radiation retrieved from Landsat 8 satellite images during 5 different overpass times when clear satellite images were available. In order to evaluate the representativeness, net radiation measured by the tower radiometer was compared with satellite retrieved net radiation aggregated over the tower footprint. Figure 5.10 shows the results of these comparisons.

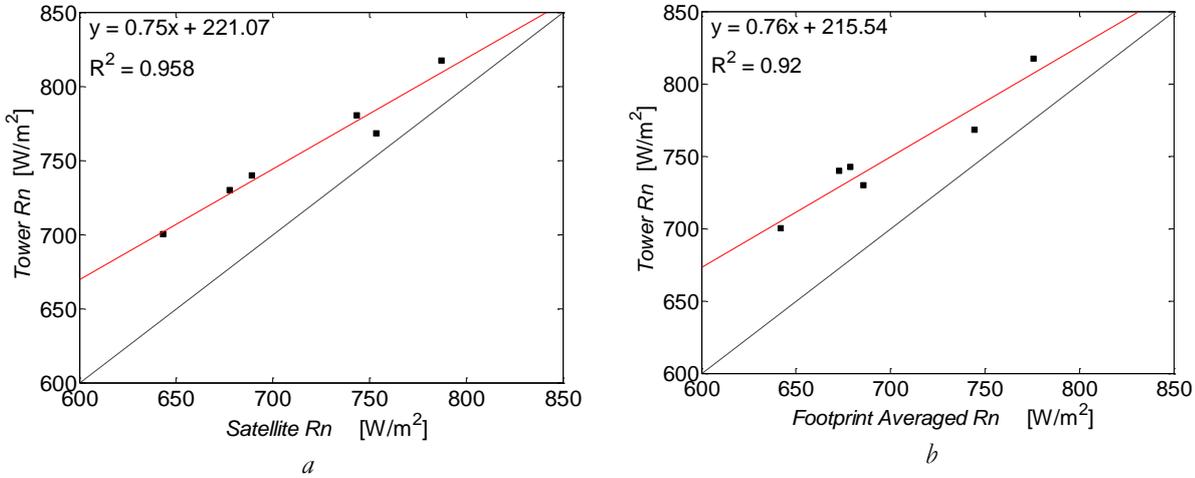


Figure 5.10: Comparisons of tower measured and satellite derived net radiation (Rn). (a) shows comparison with tower pixel value while (b) shows comparison with net radiation aggregated over the tower footprint area. The dashed line shows the 1:1 relationship.

Net radiation measured by the tower radiometer is higher than net radiation retrieved from the satellite with a mean error of  $\sim 50 \text{ W m}^{-2}$ , both for the tower pixel value and when the satellite net radiation is averaged over the tower footprint. The coefficient of determination is 0.96 for comparison between satellite derived net radiation at the tower pixel and 0.92 for comparison with net radiation averaged within the tower footprint.

To account for the over-estimation when measurements are taken at a point by the tower radiometer, a bias correction factor was computed using the formulation in Eq. 5.1

$$BF = \frac{\sum_{i=1}^{i=n} S}{\sum_{i=1}^{i=n} T} \quad 5.1$$

Where BF is the bias factor,  $S$  refers to the satellite derived net radiation (averaged over the tower footprint),  $T$  is the tower measurements and  $n$  is the number of observations. The bias factor computed following this formulation was 0.93. Tower net radiometer measurements were corrected by multiplying them with this factor; and the effect of the correction on energy balance closure was evaluated. Applying this bias factor decreases the tower measured net radiation by  $\sim 5\%$ . After correction of net radiation to account for the spatial variability, overall EBR increased by 5% for the three years (2012-2014), while individual EBRs for the years 2012, 2013, 2014 and the 2 months evaluated in 2016 increased by 11%, 4%, 12% and 7% respectively. Slopes of linear regression of H+LE vs Rn-G0 increased by 6% overall and yearly slopes increased by 5-7%. Table 5.6 shows a summary of coefficients of linear regression of H+LE vs Rn-G0 as well as EBRs after correcting for bias in net radiation.

Table 5.6: Summary of Coefficients of linear regression of H+LE vs Rn-G0, EBRs and RMSEs after correcting for bias in Rn

|   | Year                       | Slope | EBR  | RMSE<br>[W m <sup>-2</sup> ] | R <sup>2</sup> |
|---|----------------------------|-------|------|------------------------------|----------------|
| <b>Original data set<br/>with Foken et al. (2004)<br/>quality flags</b> | 2012                       | 0.73  | 0.67 | 51.23                        | 0.83           |
|   | 2013                       | 0.60  | 0.56 | 98.63                        | 0.64           |
|   | 2014                       | 0.57  | 0.51 | 94.01                        | 0.63           |
|   | 2016 (2 months)            | 0.56  | 0.49 | 61.10                        | 0.78           |
|   | <b>Overall (2012-2014)</b> | 0.63  | 0.58 | 85.61                        | 0.70           |
| <b>Correcting for bias in Net<br/>Radiation</b>                         | 2012                       | 0.80  | 0.78 | 58.87                        | 0.82           |
|   | 2013                       | 0.65  | 0.60 | 99.13                        | 0.63           |
|   | 2014                       | 0.63  | 0.63 | 101.93                       | 0.68           |
|   | 2016 (2 months)            | 0.60  | 0.56 | 71.82                        | 0.73           |
|   | <b>Overall (2012-2014)</b> | 0.69  | 0.63 | 86.31                        | 0.69           |

### 5.2.6. Combining Friction Velocity filtering, Filtering when wind direction was between 60°- 120° and Net Radiation Bias Correction.

When a combination of filtering data when  $u^* < 0.3 \text{ m s}^{-1}$ , when wind direction is between 60°- 120° and correcting for bias in net radiation is applied; the overall EBR for three years(2012 – 2014) becomes 76% which is an 18% increase from the original overall EBR of 58%. Yearly EBRs increased to 83%, 77%, 69% and 63% for 2012, 2013, 2014 and the 2 months of 2016 respectively. Despite being within closure values obtained by many authors in such areas, this closure is still low and other possible factors attributed to lack of closure that were not analysed in this study need to be evaluated. Figure 5.11 shows plots of linear regression of H+LE vs Rn-G after combined filtering.

Table 5.7: Summary of linear regressions coefficients, EBRs and RMSEs after combined filtering of data when  $u^* < 0.3 \text{ m s}^{-1}$ , filtering when wind direction between 60°- 120° and correcting for bias in net radiation

|  | Year                       | Slope | EBR  | Mean Error<br>(Wm <sup>-2</sup> ) | R <sup>2</sup> |
|--|----------------------------|-------|------|-----------------------------------|----------------|
| <b>Original data set<br/>with Foken et al. (2004)<br/>quality flags</b>  | 2012                       | 0.73  | 0.67 | 51.23                             | 0.83           |
|  | 2013                       | 0.60  | 0.56 | 98.63                             | 0.64           |
|  | 2014                       | 0.57  | 0.51 | 94.01                             | 0.63           |
|  | 2016 (2 months)            | 0.56  | 0.49 | 61.10                             | 0.78           |
|  | <b>Overall (2012-2014)</b> | 0.63  | 0.58 | 85.61                             | 0.70           |
| <b>Combined filtering:<br/><math>u^* &lt; 0.3 \text{ m s}^{-1}</math>, wind<br/>direction between 60°- 120°<br/>and correcting for bias in<br/>net radiation</b> | 2012                       | 0.83  | 0.83 | 60.81                             | 0.86           |
|  | 2013                       | 0.71  | 0.77 | 149.24                            | 0.69           |
|  | 2014                       | 0.66  | 0.69 | 127.11                            | 0.67           |
|  | 2016 (2 months)            | 0.61  | 0.63 | 63.05                             | 0.71           |
|  | <b>Overall (2012-2014)</b> | 0.74  | 0.76 | 114.73                            | 0.74           |

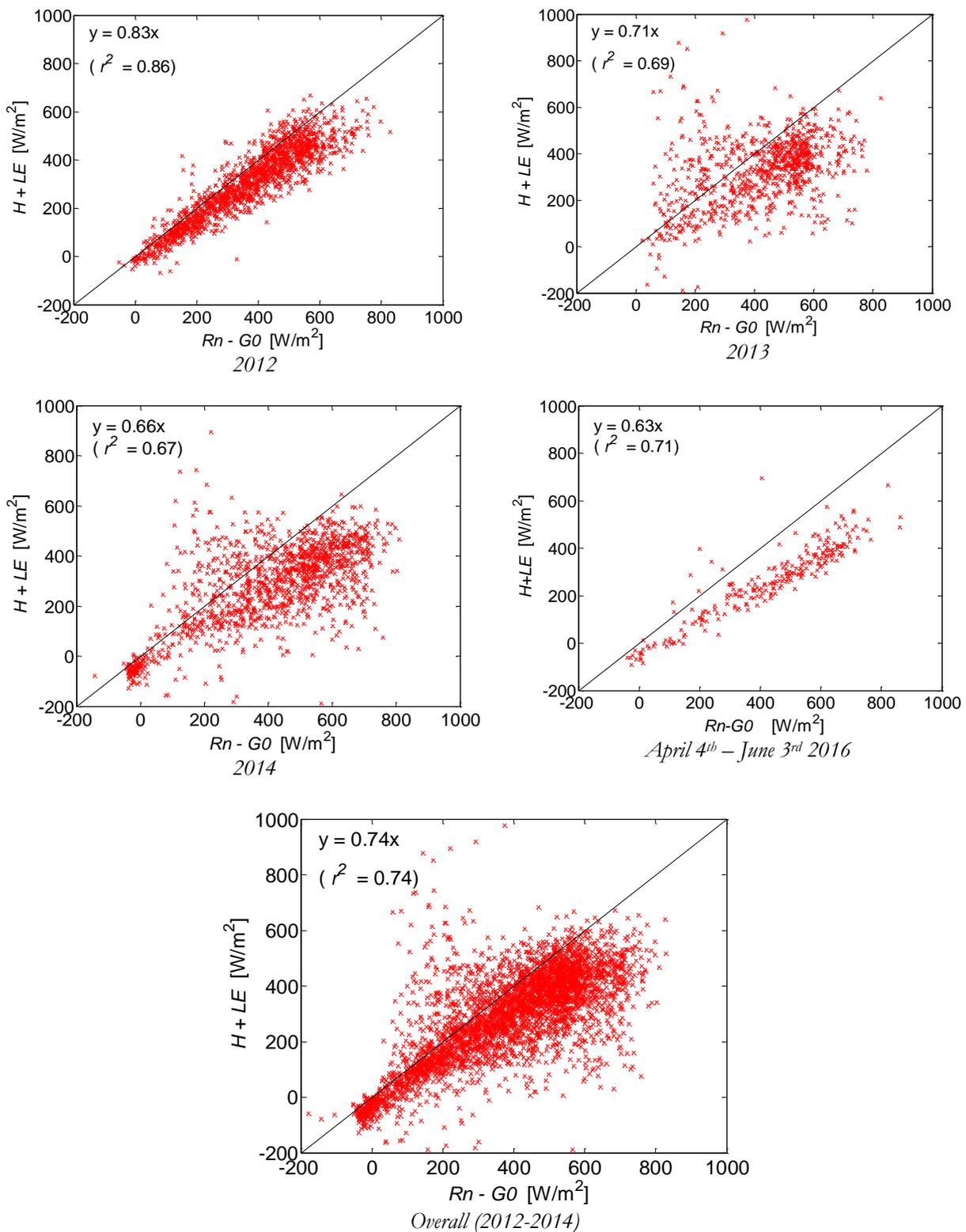


Figure 5.11: Linear regression of  $Rn-G_0$  against  $H+LE$  for the year 2012, 2013, 2014 and 2016 together with the three year overall 2012-2014; after combined filtering of data when  $u^* < 0.3 \text{ ms}^{-1}$ , when wind direction is between  $60^\circ - 120^\circ$  and correcting for the bias in net radiation. The regression lines have been forced through the origin.

**5.2.7. Comparing Energy Balance Closure using Bowen Ratio Measurements and Gas Analyzer Measurements.**

As aforementioned, the Naivasha flux tower relies on Bowen ratio measurements to derive latent heat flux. Standard eddy covariance systems use a gas analyzer which relies on the eddy covariance theory for direct measurements of latent heat. The disadvantage of Bowen ratio method is that it may not be able to capture small temperature and humidity gradients. Figure 5.12 shows comparison of latent heat flux derived using the Bowen ratio method with latent heat measured using a gas analyzer for the short period that the gas analyzer was installed in 2012.

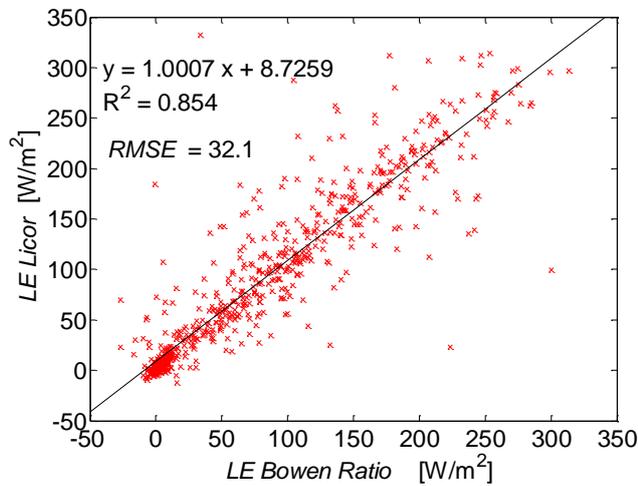


Figure 5.12 Comparison between Latent heat from Bowen ratio and latent heat measured by a gas analyzer for the days the gas analyzer was working

Latent heat measured using the gas analyzer is slightly higher than latent heat derived using Bowen ratio. The coefficient of determination ( $R^2$ ) is 0.85, and the RMSE is 32.1. The Bowen ratio therefore underestimates Latent heat flux for this site.

Energy balance closure was analyzed separately using LE measured with the gas analyzer and LE derived from Bowen ratio for the period when the gas analyzer operated. Figure 5.13 shows plots of linear regression of  $H+LE$  vs  $Rn-G_0$  using LE measured by gas analyzer and using LE derived from Bowen ratio.

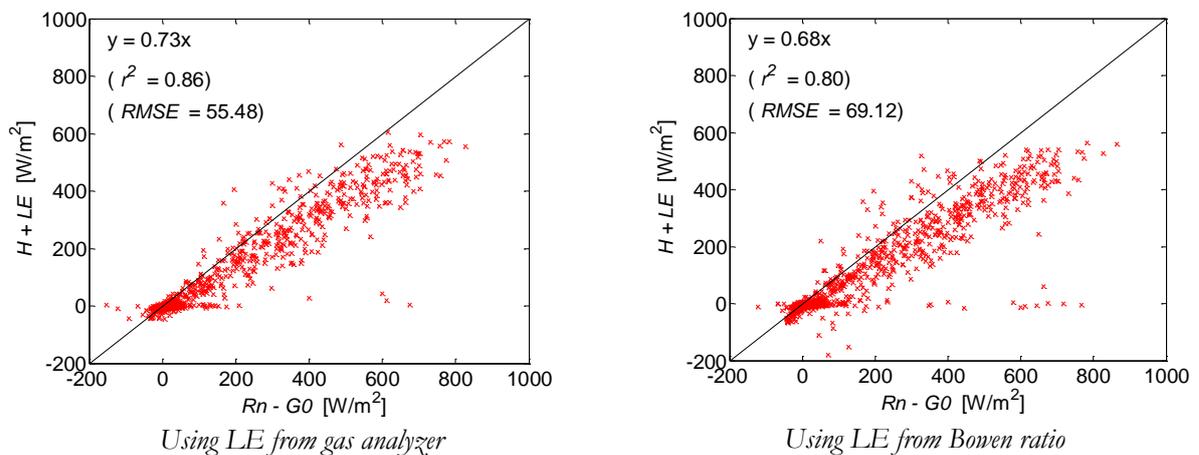


Figure 5.13: Linear regressions of  $H+LE$  vs  $Rn-G_0$  using LE measured by gas analyzer and using LE derived from Bowen ratio.

The EBR using LE measured by the gas analyzer was 77% compared to 66% when LE was derived using Bowen ratio for the same period. Slopes of linear regression gave closures of 73% using LE measured by the gas analyzer and 68% using LE derived from Bowen ratio. Figure 5.14 shows linear regressions of H+LE vs Rn-G0 after combined data filtering discussed in Section 5.2.6.

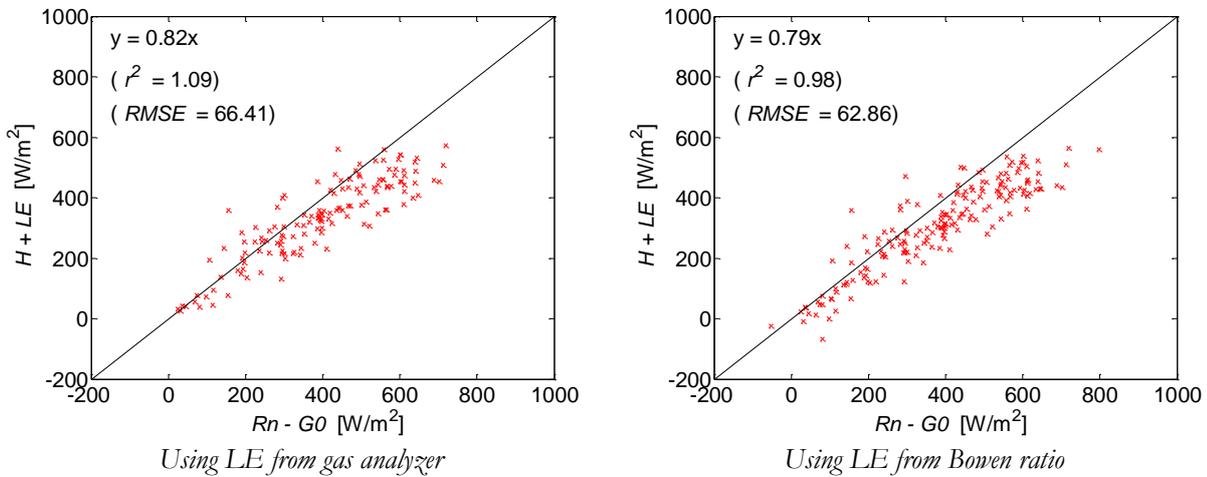


Figure 5.14: Linear regressions of H+LE vs Rn-G0 using LE measured by gas analyzer and using LE derived from Bowen ratio after combined data filtering discussed in Section 5.2.6

Using combined data filtering discussed in Section 5.2.6 improved the EBR calculated using LE measured by the gas analyzer to 84%, while EBR improved to 80% when using LE derived from Bowen ratio. The slopes show closures of 82% and 79% well within the EBR ranges.

## 6. CONCLUSION AND RECOMMENDATIONS

### 6.1. Conclusion

This research was mainly aimed at analyzing the causes of low energy balance closure using measurements taken from a flux tower situated in a semi-arid savannah area in Naivasha, Kenya.

The three year overall energy balance ratio (EBR) was 58% , while yearly closures were 67% for 2012, 56% for 2013, 51% for 2014 and 49% for 2 months analysed in 2016. Quality filtering of fluxes when  $u^*$  was less than  $0.3 \text{ m s}^{-1}$  improved the overall EBR for the three years evaluated by 5%. The flux footprint slightly extends into the nearby urban area towards the North and to the road surface towards the east of the tower. Filtering data containing fluxes from the road surface when wind direction is between  $60^\circ - 120^\circ$ , improved the EBR by 6%. Net radiation measured by the tower radiometer is higher than net radiation retrieved from Landsat 8 satellite both at the tower pixel and when averaged over the flux source area. Correcting for the bias in net radiation improved the overall EBR by 5%. Combining filtering data when  $u^* < 0.3 \text{ m s}^{-1}$ , when wind direction is between  $60^\circ - 120^\circ$  and correcting for bias in net radiation improved the overall EBR for three years (2012 – 2014) to 76% which is an 18% increase. Yearly EBRs increased to 83%, 77%, 69% and 63% for 2012, 2013, 2014 and the 2 months of 2016 analyzed respectively. Despite being within closure values obtained by many authors in such areas, other possible factors attributed to lack of closure that were not analysed in this study need to be evaluated.

There is a systematic reduction in energy balance closures over the years which may be due to deterioration of Bowen ratio measuring equipment. Inter-calibration did not however improve the energy balance closure as it was expected. On the other hand, using a gas analyzer for latent heat flux measurements gives higher energy balance closures for the site than using Bowen ratio by.

There is a possibility of an error in estimation of ground heat flux due to lack of representativeness when only one soil heat flux plate is used to estimate ground heat flux.

### 6.2. Recommendations

1. Other factors attributed to lack of closure such as advection and averaging time that were not analysed in this study need to be evaluated.
2. A gas analyzer should be added to the tower for more accurate measurements of Latent heat fluxes.
3. For quantitative analysis of the effect of estimating ground heat fluxes using soil heat flux plate measurements in different directions on the energy balance closure, temperature profiles should be separately measured at each plate location, rather than relying on diffusivity estimated from only one location.



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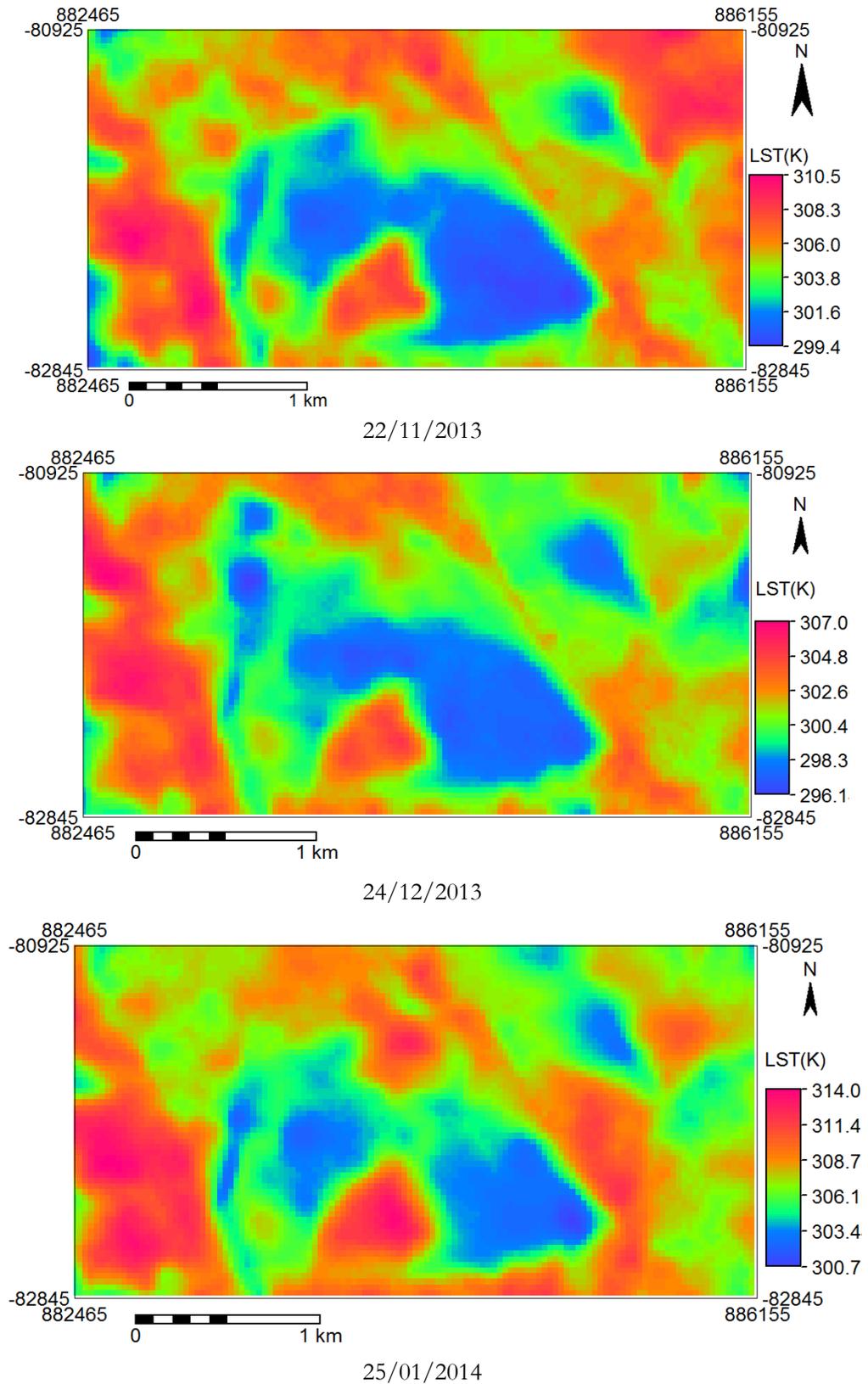
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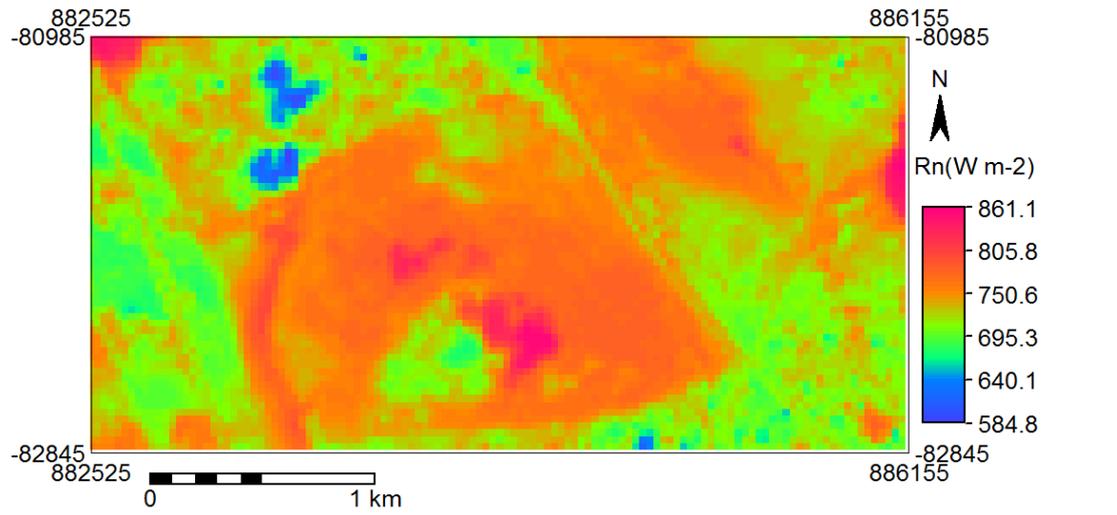
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# APPENDICES

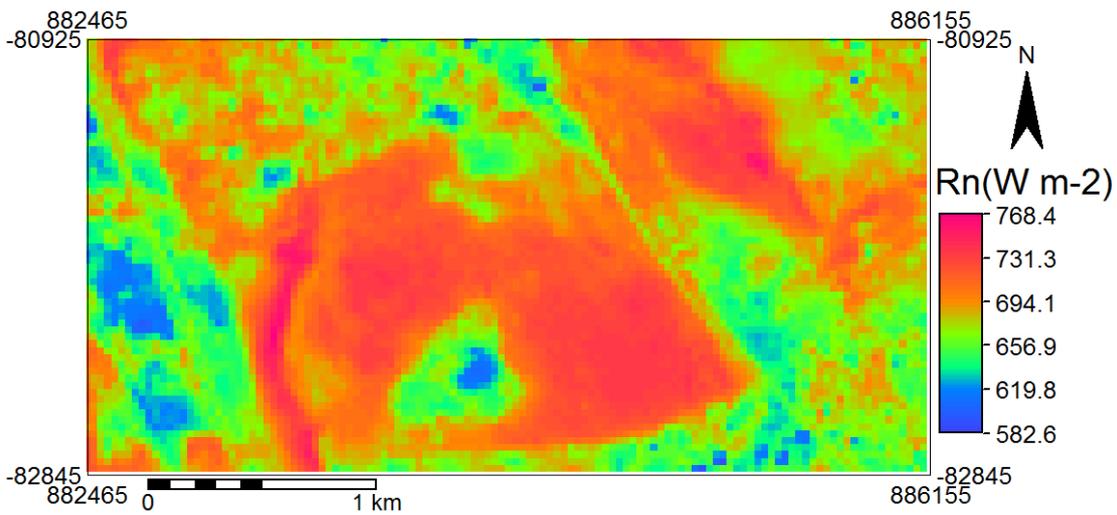
## Appendix A. Land Surface Temperature Maps Derived Using the Single Channel Algorithm



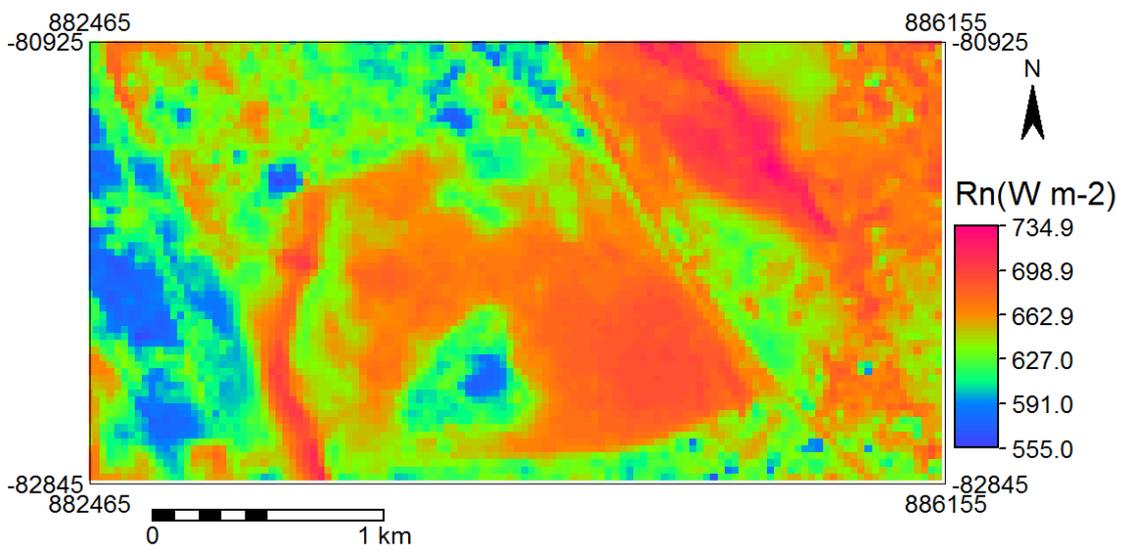
Appendix B. Net Radiation Maps derived from Landsat 8 OLI & TIRS for the study area.



24/12/2013



25/01/2014



02/06/2014